Fair Tree

Fairshare Algorithm for Slurm

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Outline

- Introduction to job prioritization
- BYU's setup
- Issues with existing fairshare algorithms
- Fair Tree
- Fairshare=parent on accounts
- Appendix

Job Prioritization

- Job Priority can include different components:
 - Age
 - JobSize
 - Partition
 - QOS
 - Fairshare this is what we will discuss
- Job Priority = sum(ComponentWeight * ComponentFactor)
 - Weight is an integer
 - Factor is between 0.0 and 1.0
- Job Priority = 1000 * 0.34 + 5000 * 0.12 + 2000 * 0.54

Fairshare Factor

- Usage and Shares are the two components of Fairshare Factor
- Raw Shares are assigned to each association by an admin
 - "Shares" is Raw Shares when normalized to 0.0 .. 1.0
 - Similar to slices of a pie
 - Represents the part of the system that is "yours"
- "Usage" is a value between 0.0 and 1.0 that represents your proportional usage of the system

Fairshare Equation

Basic premise of fairshare:

If Shares == Usage, you have hit your "fairshare target"

Fairshare Equation

Fairshare Factor = 2^{-Usage/Shares}

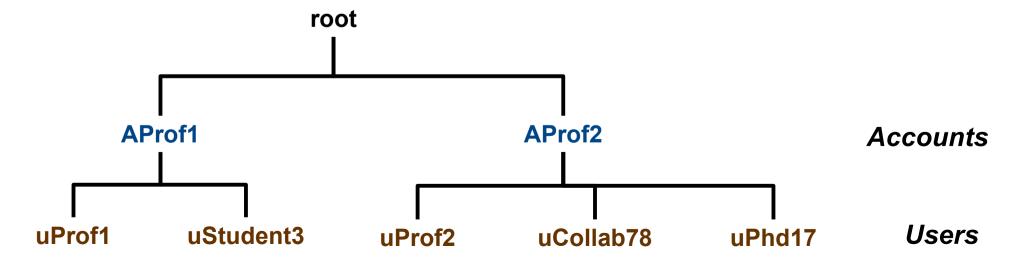
or

$$F = 2^{-U/S}$$

- Result is between 0.0 and 1.0
- When Usage increases, F decreases
- When Usage decreases, F increases

BYU's Setup

- Each professor has a Slurm account
 - Has account coordinator status for that account
 - BYU doesn't charge \$\$\$ for usage
 - Accounts are treated equally (Shares are the same)
- Students and collaborators are users in a professor's account
 - Users are treated equally (Shares are the same, unless account coordinator changes them)



Our Definition of "Fair"

- If accounts A and B are siblings and A has a higher fairshare factor than B, all children of A will have higher fairshare factors than all children of B
 - True for all sibling associations at all levels

Disclaimer

- We will discuss BYU's use case and how to support it
 - It may also apply to many other use cases
- We are building on the hard work of others
- We identified some issues with existing algorithms but our work would not have been possible without the other algorithms

New Fairshare Algorithm

We wrote a new fairshare algorithm.



The Problem

Account with 35% usage had higher priority than accounts with only 10% usage

Fairshare Equation

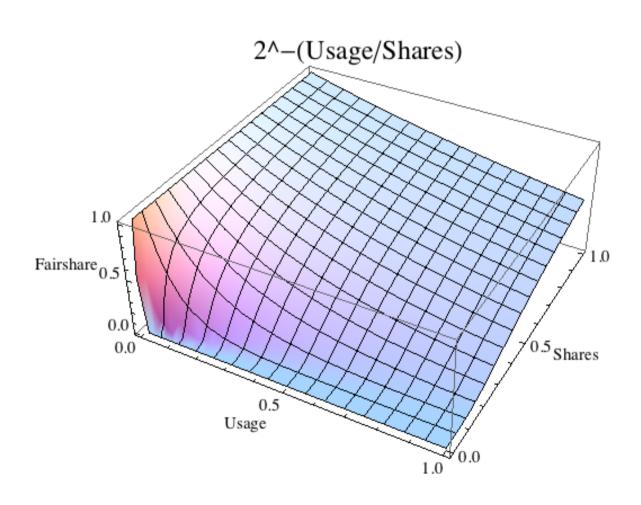
Fairshare Factor = 2^{-Usage/Shares}

or

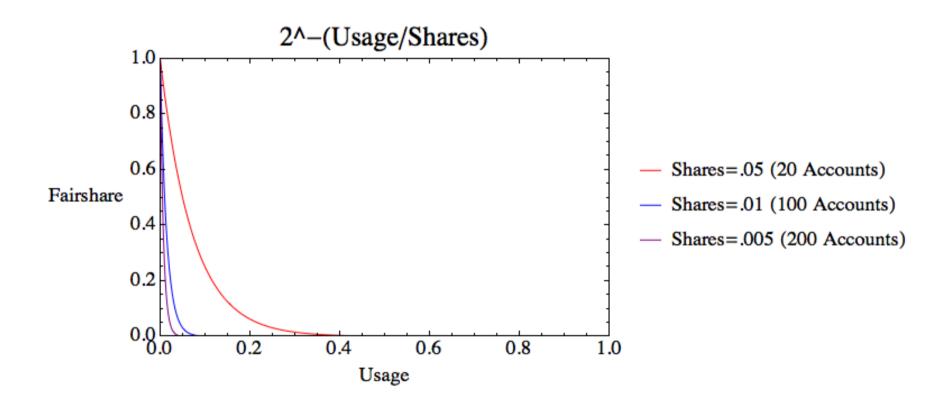
$$F = 2^{-U/S}$$

The following slides show graphs of this equation with various U and S values

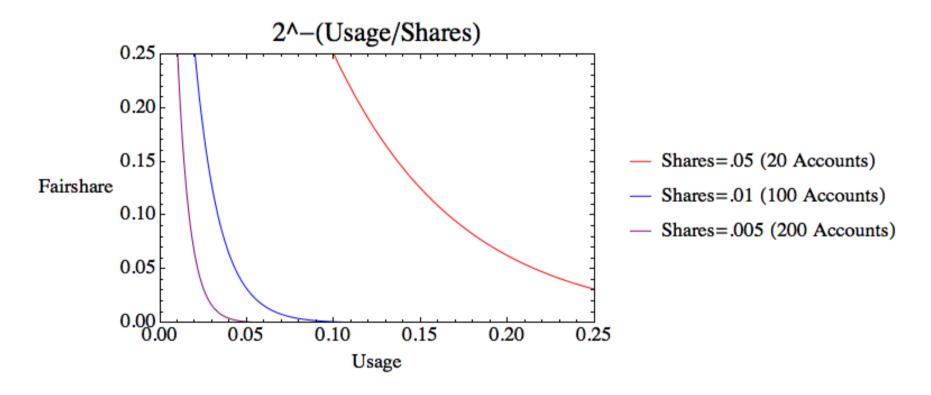
Fairshare 3D Graph



Fairshare Graph

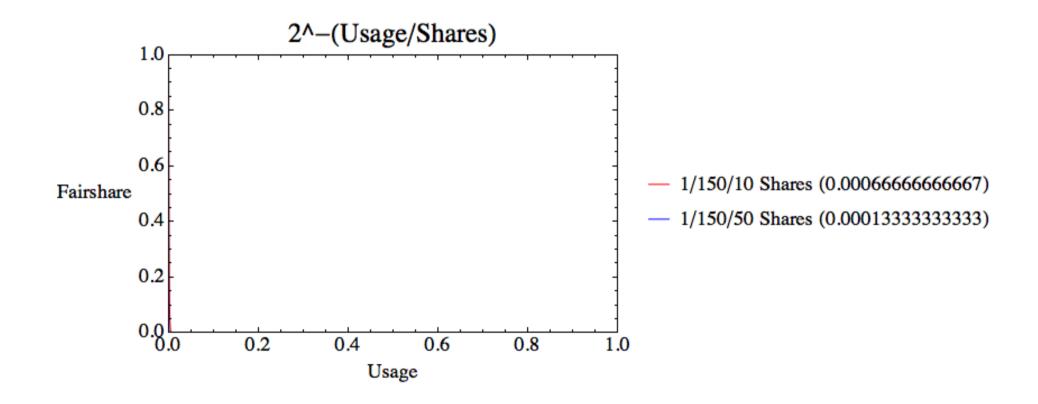


Fairshare Graph Zoomed

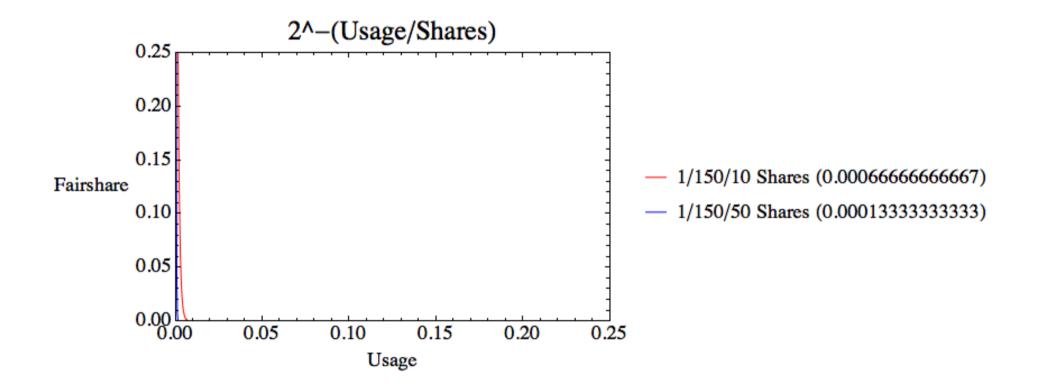


- As Usage increases, fairshare decreases
- As Shares decreases, the point at which the line visually hits the x-axis is earlier and earlier
 - At some point it will also become zero in floating point

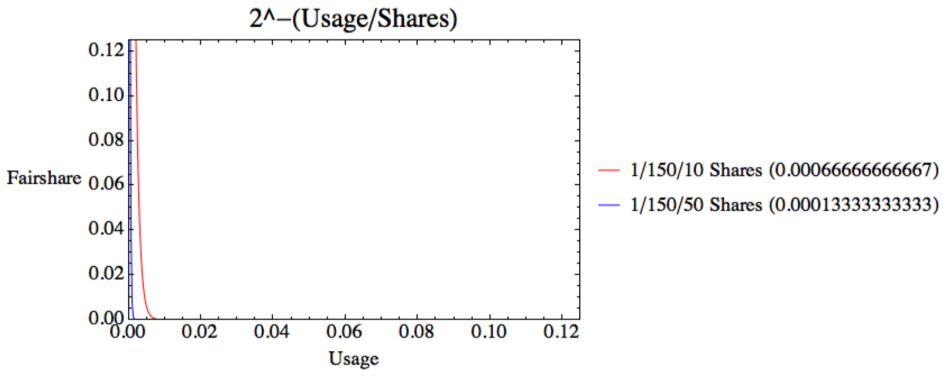
Actual Fairshare Graph



Actual Fairshare Zoomed



Actual Fairshare More Zoomed



- The Shares values were seen in production at BYU
- 150 accounts with either 10 or 50 users in an account
- Even if the Shares value is the same, the Fairshare value may be the same (zero) even with a large disparity in Usage
- Since F was zero beyond a certain point, large disparities in usage resulted in same F value

Dampening Factor

- Added in 14.03
- 2^-((Usage/Shares)/Damp)
 - Damp is a positive integer (slurm.conf)
- Great idea
- Isn't a complete solution
 - Small values may still be too small
 - Requires manual guess and check
- Can be replaced by linear interpolation
 - Ticket-Based can use this instead of MAX()
 - See Appendix

Problem With Shares Calculation

Normalized Shares equation (the "S" in 2^-(U/S)) for all current algorithms:

```
S = (RawShares_{user} / RawShares_{siblings}) * 1/4 * 
(RawShares_{account} / RawShares_{sibling-accounts}) * 1/10 * 
(RawShares_{parent} / RawShares_{parent-siblings}) * ... 1/20 * ... 1/20 * ...
```

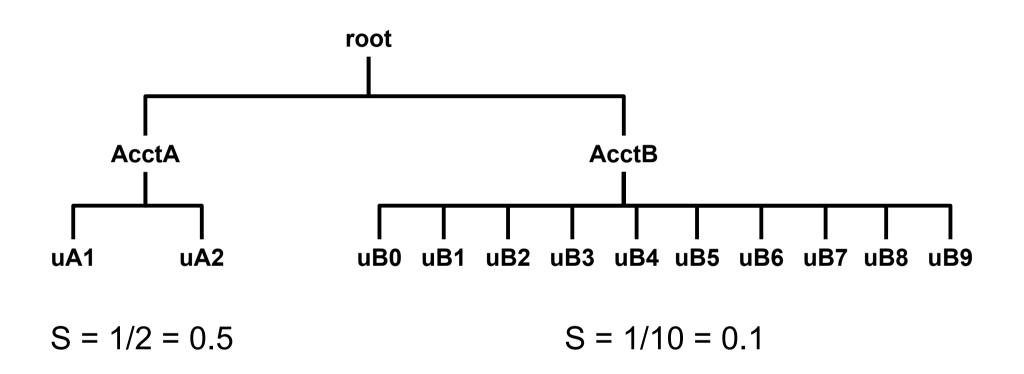
Assume sibling associations have the same Raw Shares, tree has 2 levels:

Equivalent to:

S = (1 / number of users in account) * constant

• See appendix for demonstration of equivalence

Problem With Shares Calculation



- The S values are multiplied by the same constant, thus the constant can be discarded for comparison purposes
- The S value ensures that AcctA has a huge advantage solely because it has fewer users
- End-users should attempt to get team members fired or preferably reassigned to a competing research group so that their own S increases while their competitors' S values decrease
- Problem applies to more complicated scenarios but is harder to model

Usage Effective

- Usage Effective (the U in 2^-(U/S)) =
 UA_{child}+((UE_{parent}-UA_{child})*S_{child}/S_{all_siblings})
- Assuming two levels in the tree, 2^-(U/S) expands to:

$$2^{-\left(\frac{U_{User}}{U_{Total}} + \left[\frac{U_{Acct}}{U_{Total}} + \left(1 - \frac{U_{Acct}}{U_{Total}}\right) * \frac{S_{Acct}}{S_{Acct} + S_{ASiblings}} - \frac{U_{User}}{U_{Total}}\right] * \frac{S_{User}}{S_{User} + S_{USiblings}}}\right)}{\frac{S_{User}}{S_{User} + S_{USiblings}}} * \frac{S_{Acct}}{S_{Acct} + S_{ASiblings}}}$$

- Has some unpleasant side effects that we consider bugs
 - (Have 20 minutes and a whiteboard? Let's talk!)

Other Algorithms

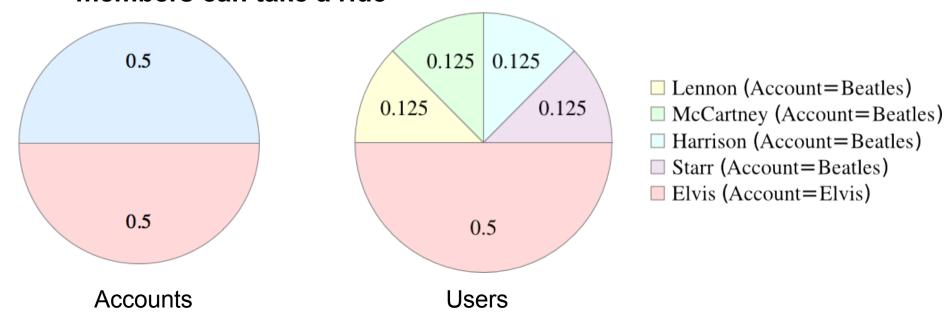
- Ticket-Based
 - Depends on queue state
 - Hard to explain to users
 - T = T_{parent} * S * F / SUM(S*F)_{active_siblings}
 - Similar issues to Norm Shares equation because (S * F / SUM(S*F)_{active_siblings}) depends on the number of active users in an account
- Depth Oblivious
 - Very complex math
 - Hard to explain to users and admins
 - Hard to evaluate its fairness
 - Many opportunities for floating point precision issues

An Example



Timeshare on a Spaceship

- The Beatles and Elvis split the cost of a spaceship and crew
- One passenger spaceship
- Elvis pays 50%
- Beatles pay 50%
 - Each member pays 25% of the Beatles' 50% (equals 1/8 of the total)
 - If a band member isn't waiting to use the spaceship, other band members can take a ride



How well does Slurm perform in this scenario?

What actually happens?

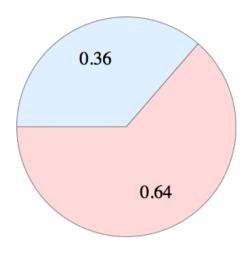
Simulated using the following account hierarchy:

	Account	User	Norm Shares
root			0.00000
beatles	3		0.500000
beatle	es	harrison	0.125000
beatle	es	lennon	0.125000
beatle	es	mccartney	0.125000
beatle	es	starr	0.125000
elvis			0.500000
elvis		elvis	0.500000

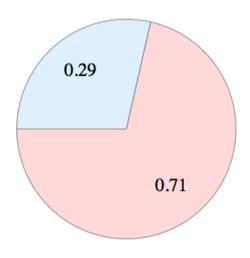
Simulation Rules

- Elvis always has work queued
- n Beatles always have worked queued
- The other Beatles do not queue any jobs
- Only one core available
- Usage and fairshare calculations run in between each job
- The following pie charts show the percentage of the system that each account used

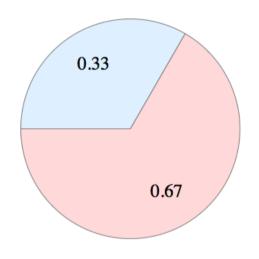
Traditional Multifactor



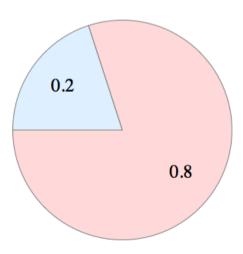
4 Beatles vs Elvis



2 Beatles vs Elvis



3 Beatles vs Elvis

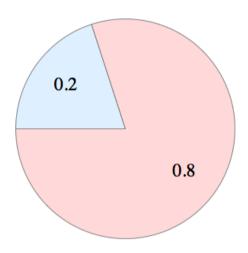


1 Beatle vs Elvis

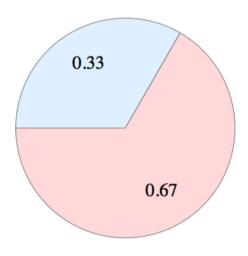




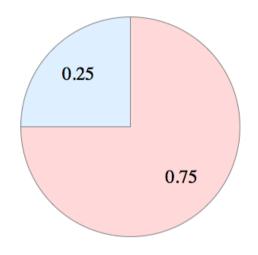
Ticket-Based



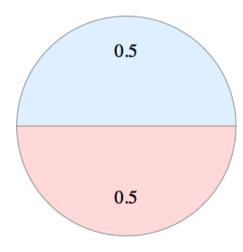
4 Beatles vs Elvis



2 Beatles vs Elvis



3 Beatles vs Elvis

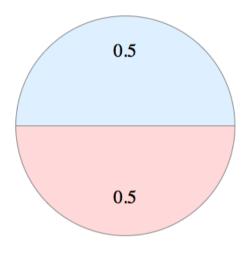


1 Beatle vs Elvis

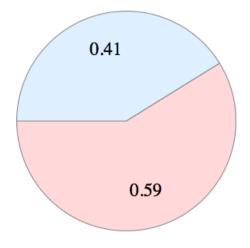




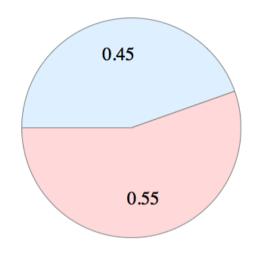
Depth Oblivious



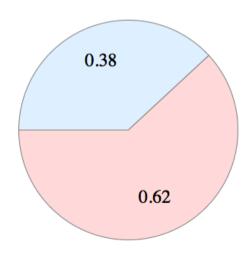
4 Beatles vs Elvis



2 Beatles vs Elvis



3 Beatles vs Elvis

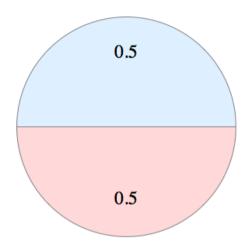


1 Beatle vs Elvis

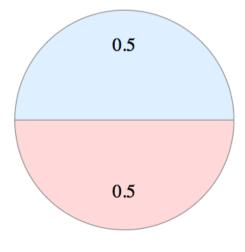




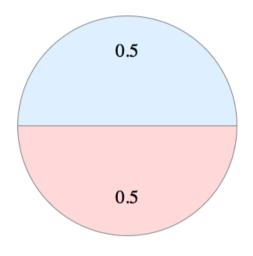
Fair Tree



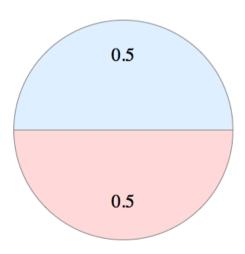
4 Beatles vs Elvis



2 Beatles vs Elvis



3 Beatles vs Elvis



1 Beatle vs Elvis



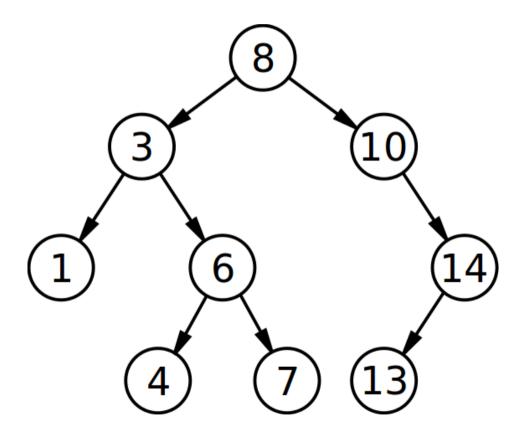


Goals of Fair Tree

- If accounts A and B are siblings and A has a higher fairshare factor than B, all children of A will have higher fairshare factors than all children of B
 - True for all sibling associations at all levels
- Eliminate problems due to floating point precision loss
- sshare and debug support

Trees

• Similar idea to binary search tree:



- Nodes are sorted
- In-order traversal results in a sorted list

Fairshare Calculation

- Level Fairshare = S / U
 - S = RawShares_{self} / RawShares_{self+siblings}
 - U = RawUsage_{self} / RawUsage_{self+siblings}
- Range: [0, infinity]
 - if U == S then LF = 1.0
- Replaces 2^-(U/S)
- Only used for sorting

Tree Traversal

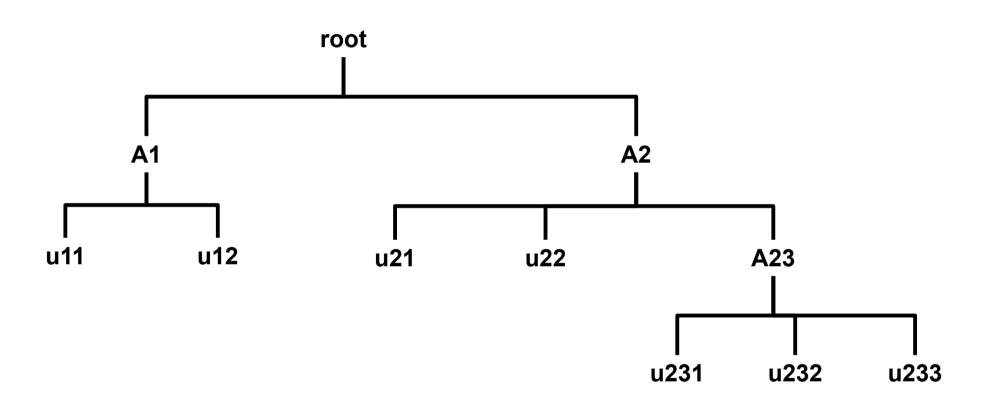
- Create "rooted plane tree"
- Traversal function, starting at root:
 - Calculate Level Fairshare for each child (S/U)
 - Sort children by Level Fairshare from highest to lowest
 - Visit the children in order
 - If account, recurse with account as new root
 - If user, assign a final fairshare factor based on ranking
- Final fairshare factor is: rank-- / user_count
 - rank is initialized to user_count
 - Ties are allowed

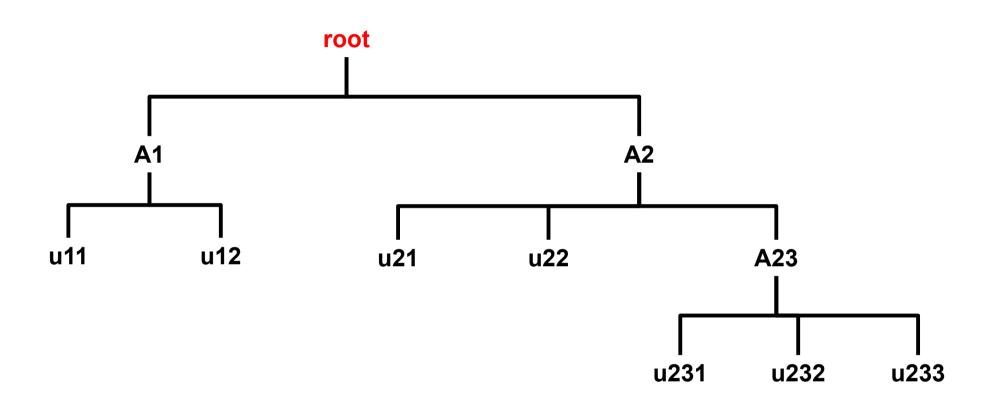
Traversal in the Fair Tree Algorithm for Slurm

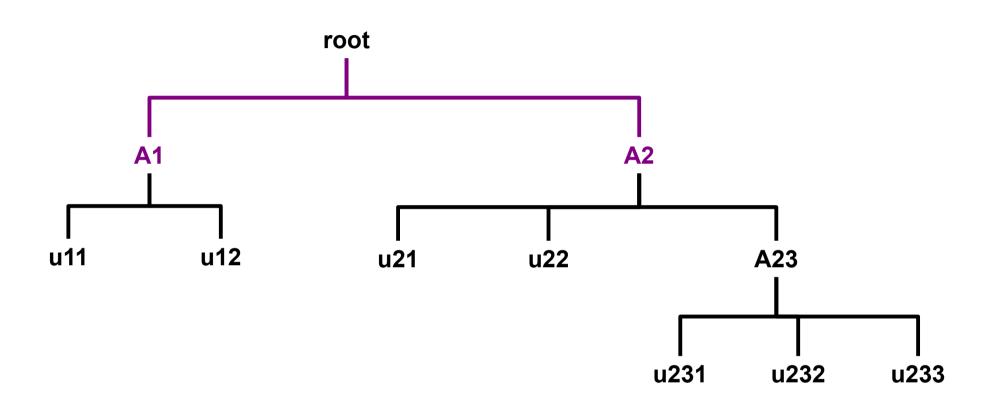
- = visit association
- = calculate level fairshare

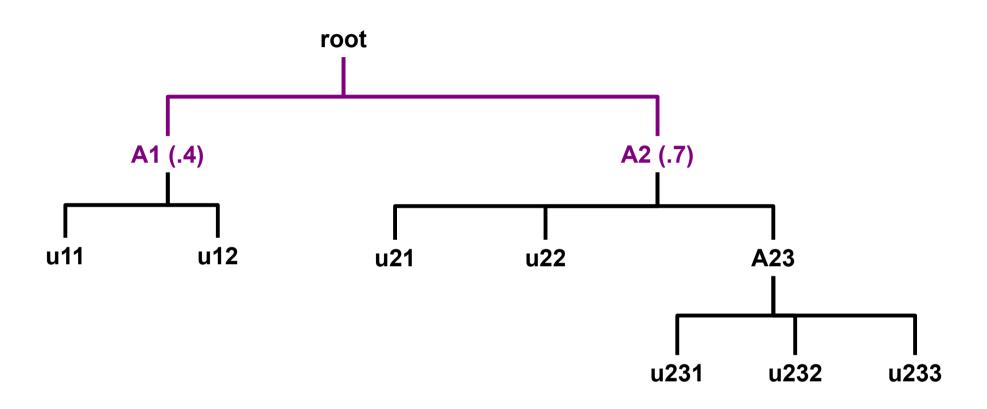
= sort siblings

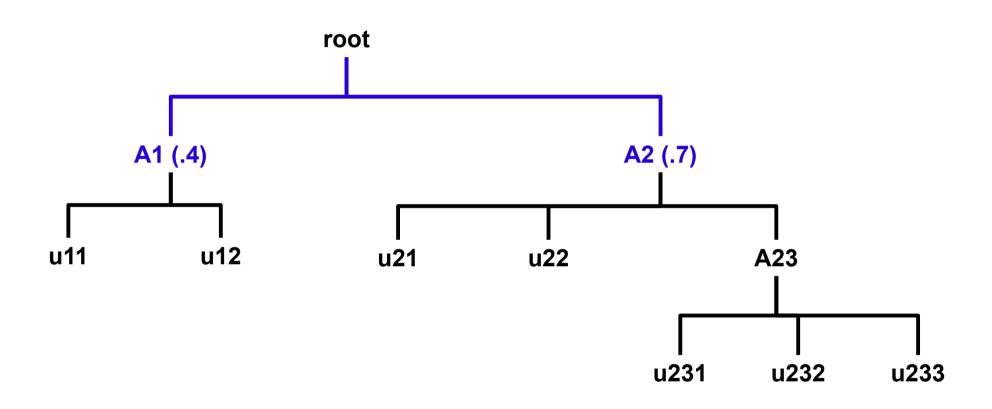
= calculate final fairshare for user

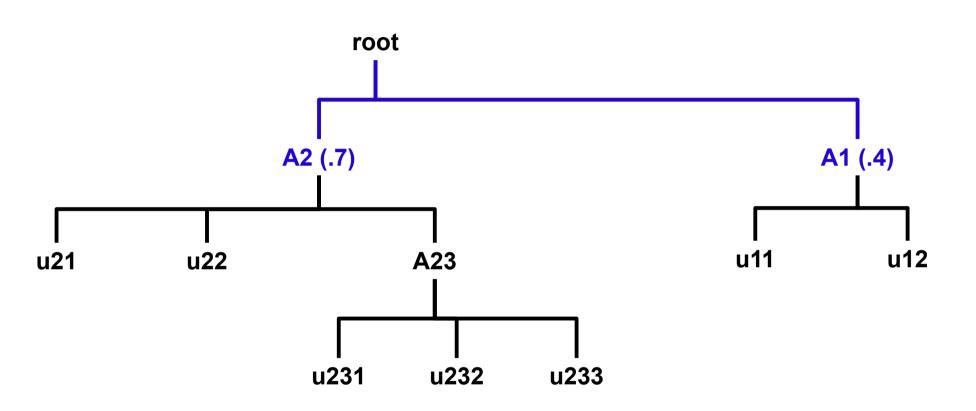


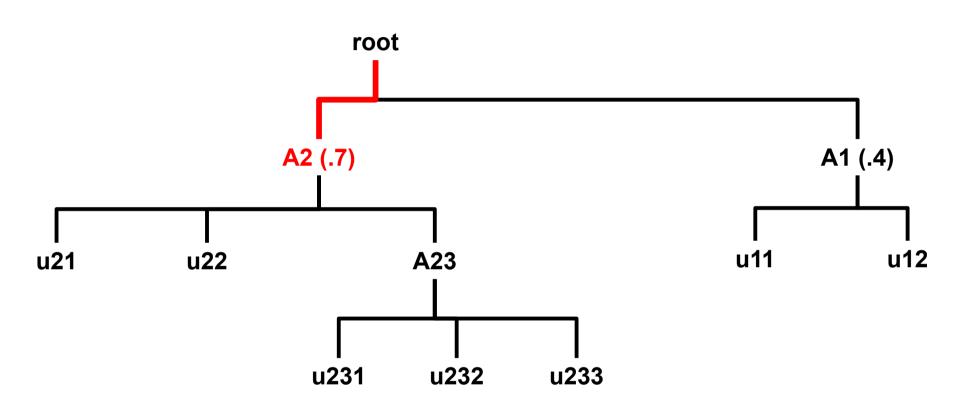


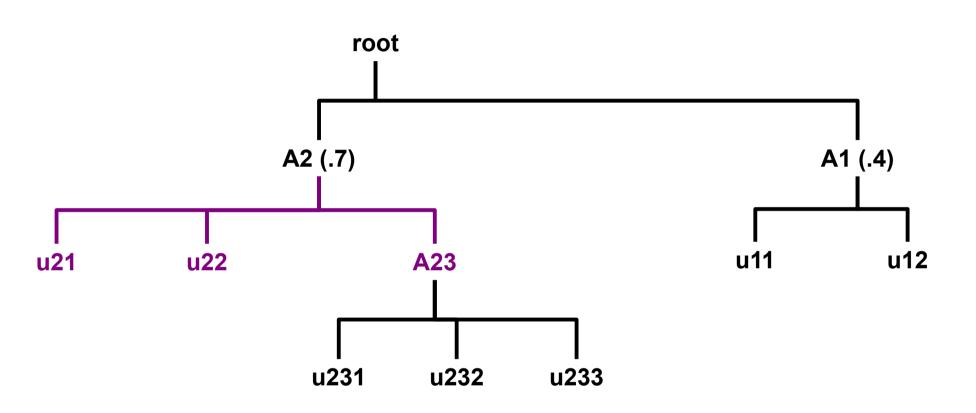


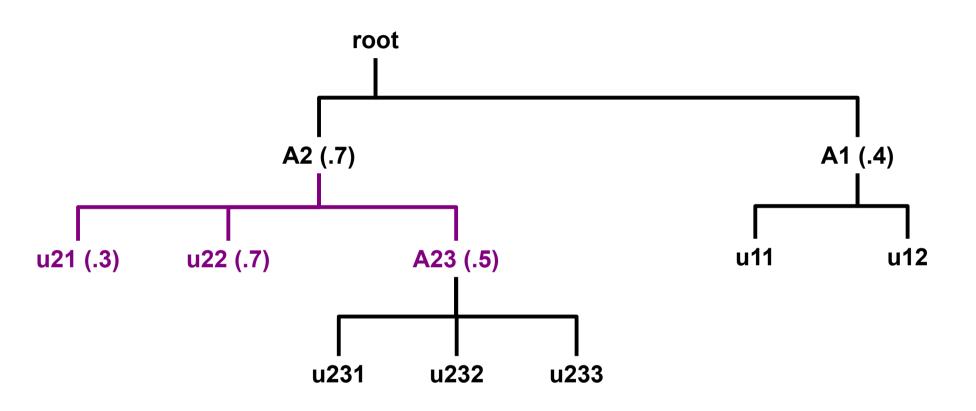


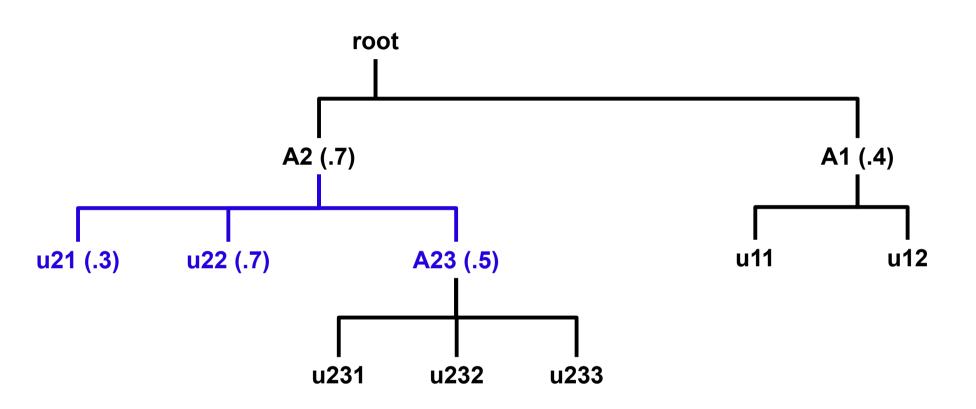


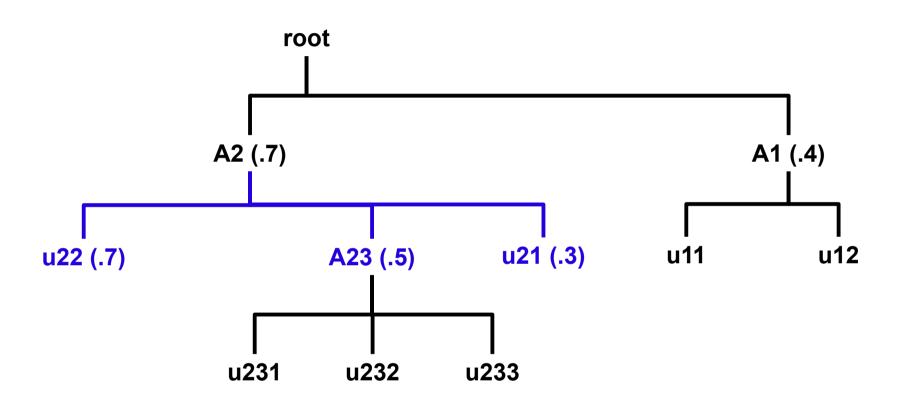


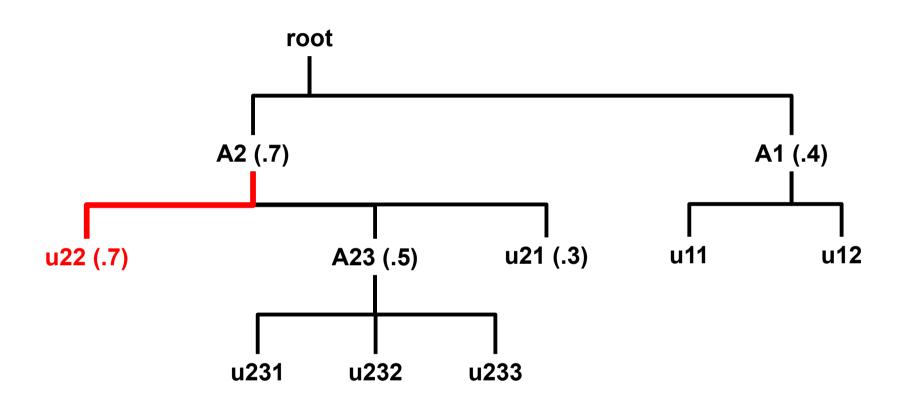


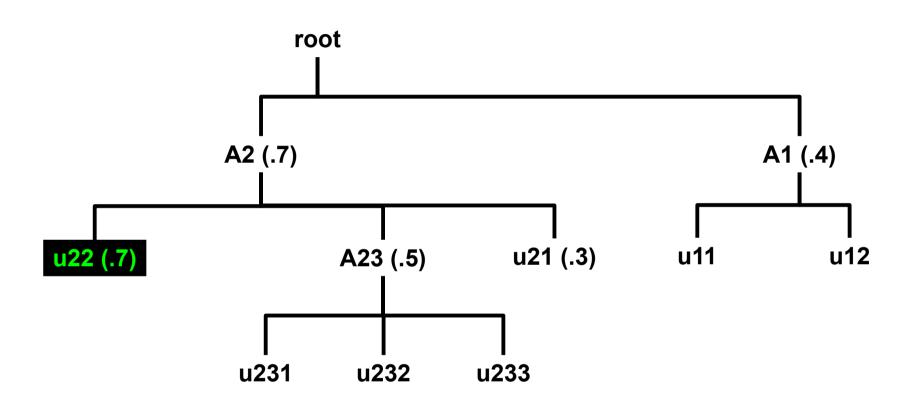




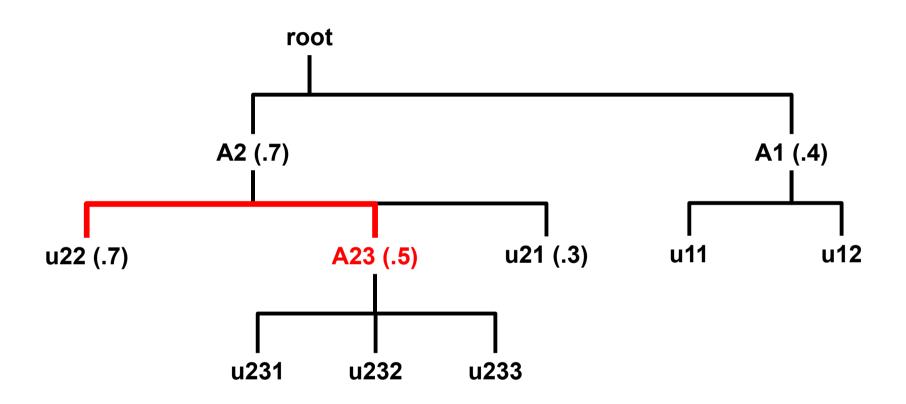


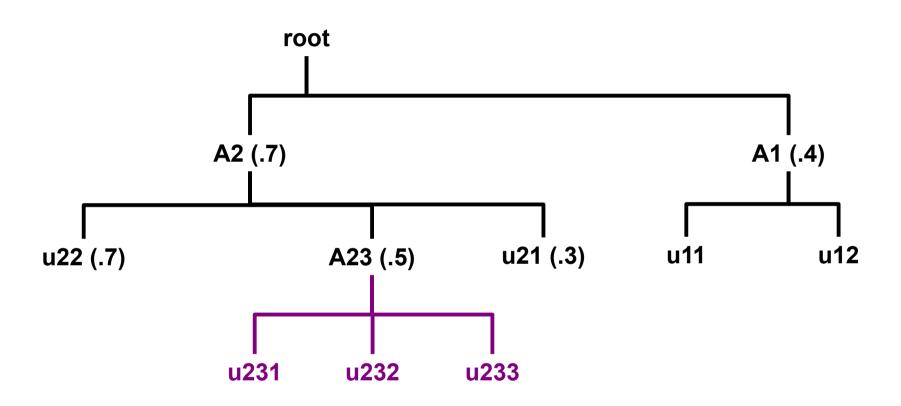


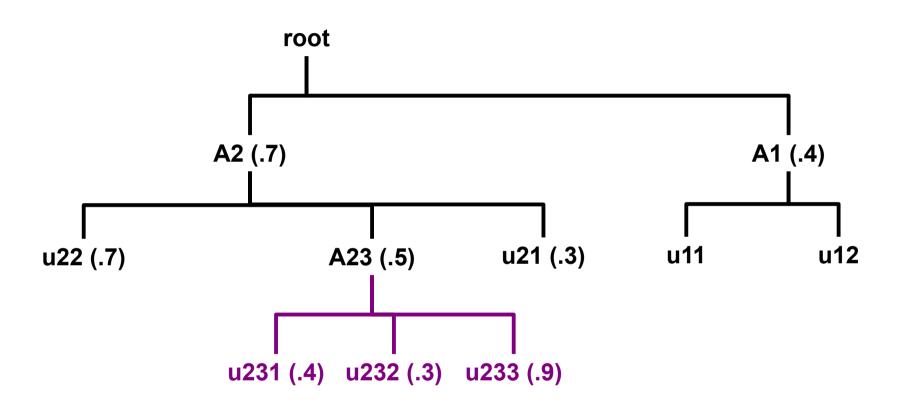


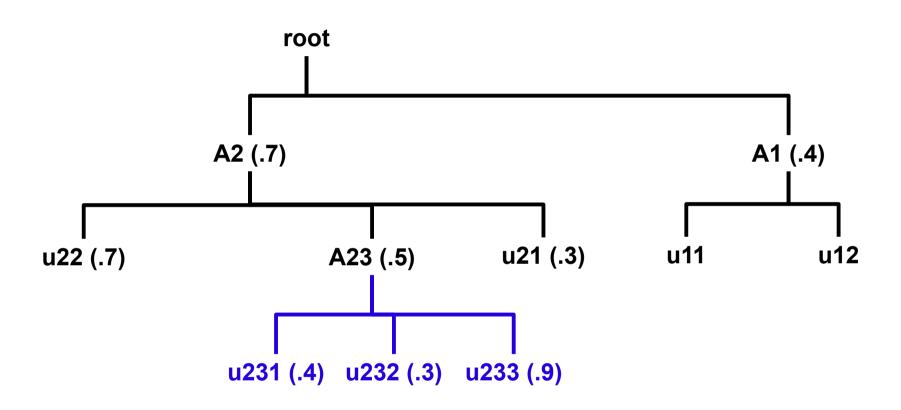


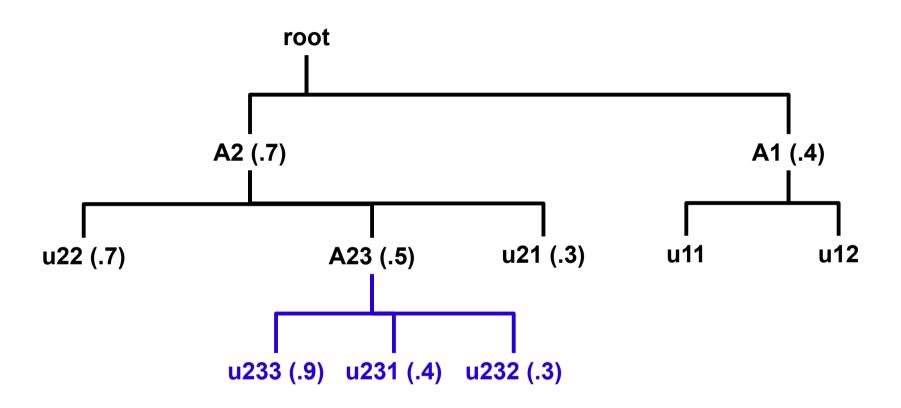
$$1.0 = 7/7$$

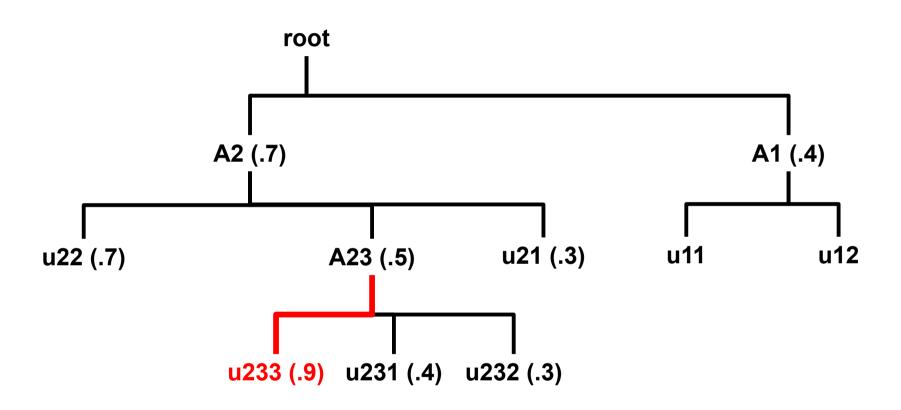


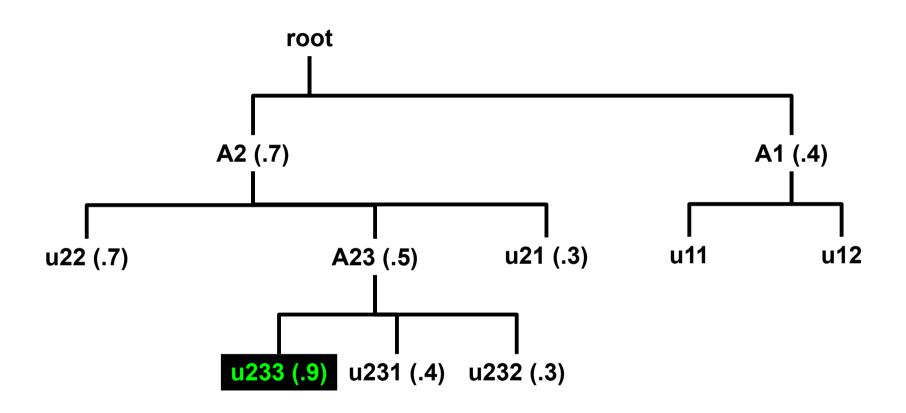




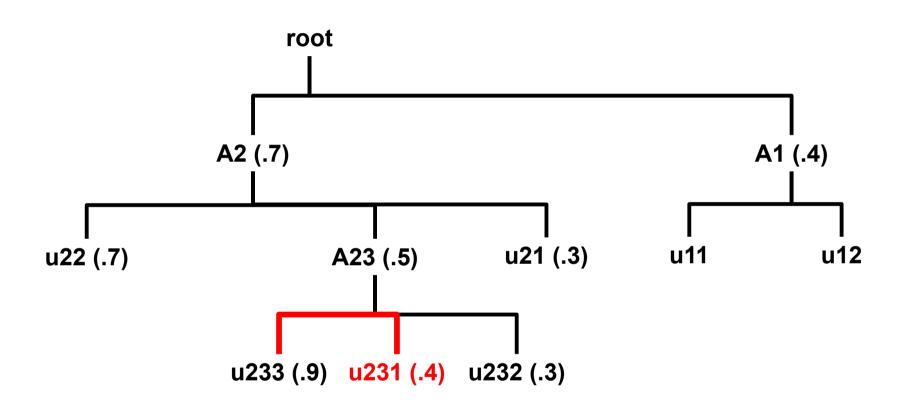


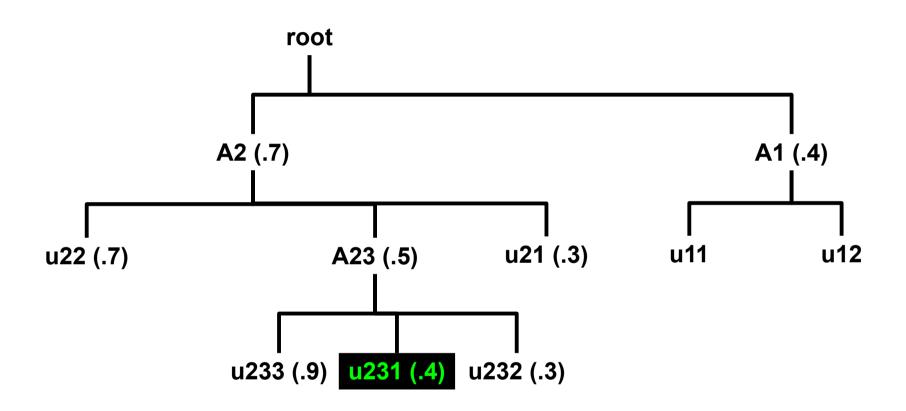




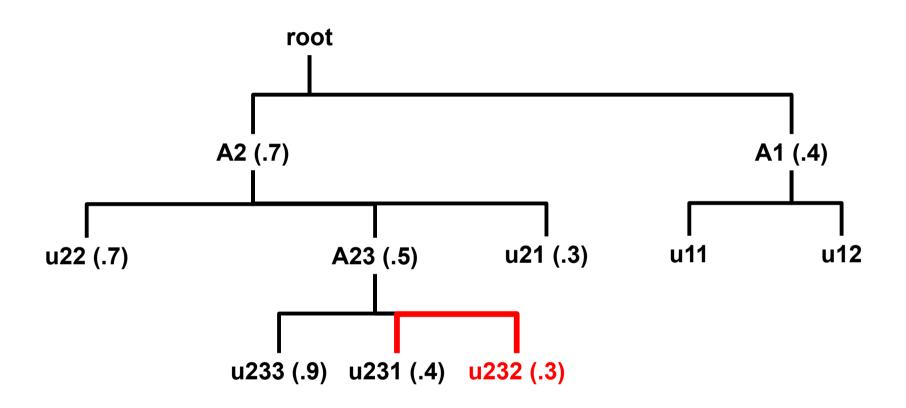


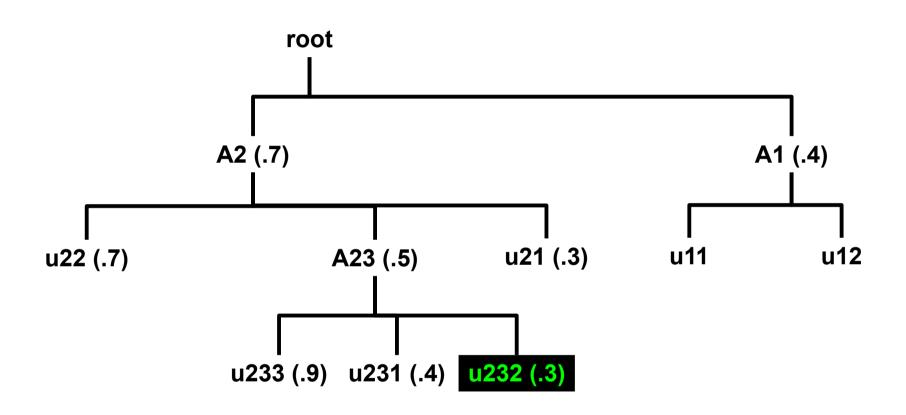
$$0.857 = 6/7$$



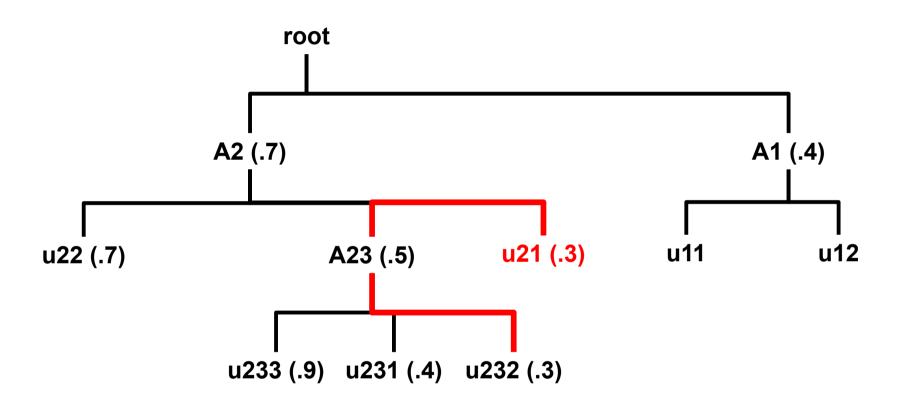


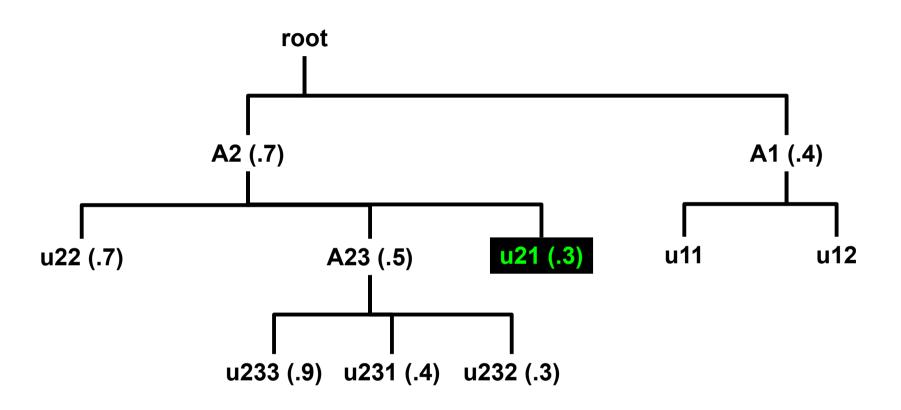
$$0.714 = 5/7$$



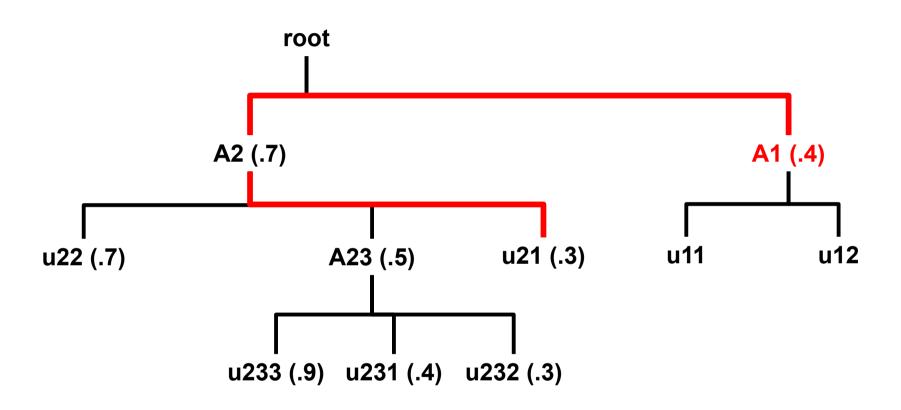


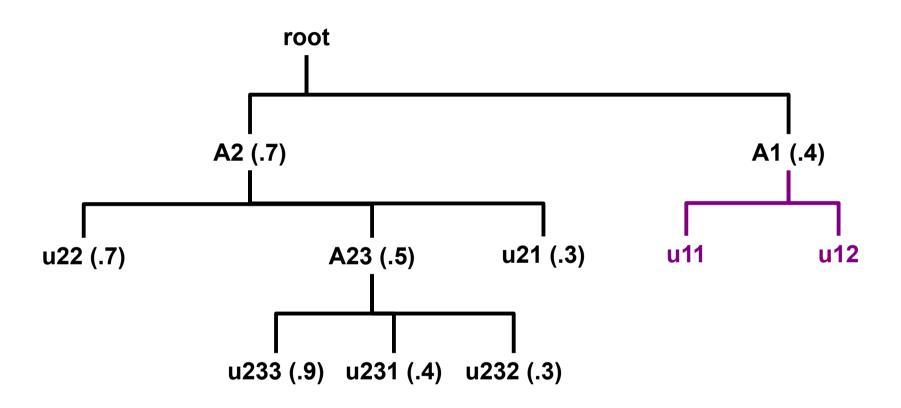
$$0.571 = 4/7$$

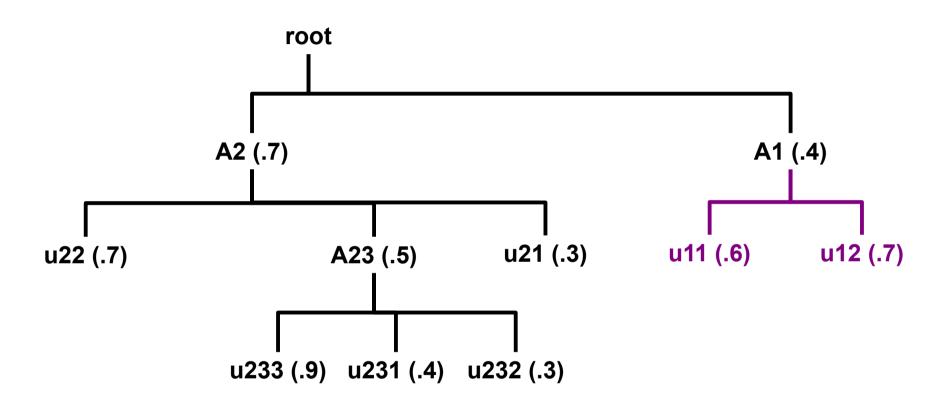


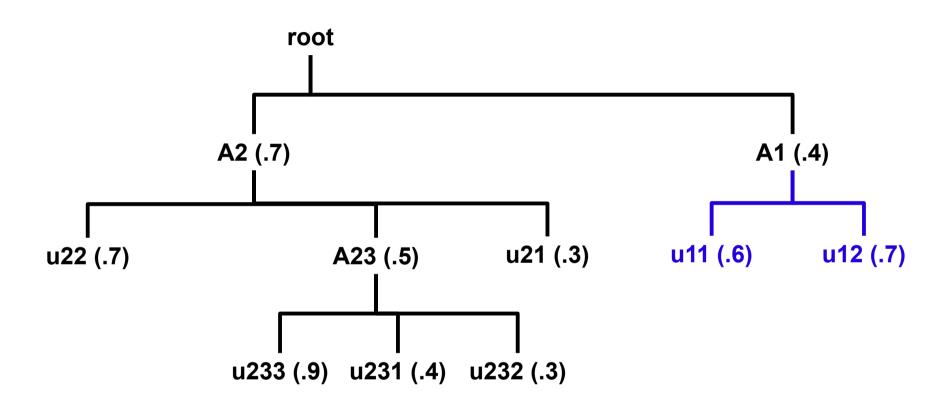


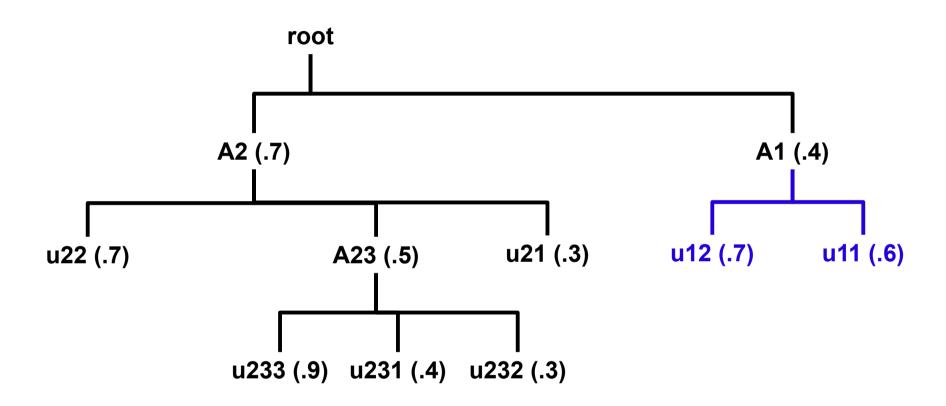
$$0.429 = 3/7$$

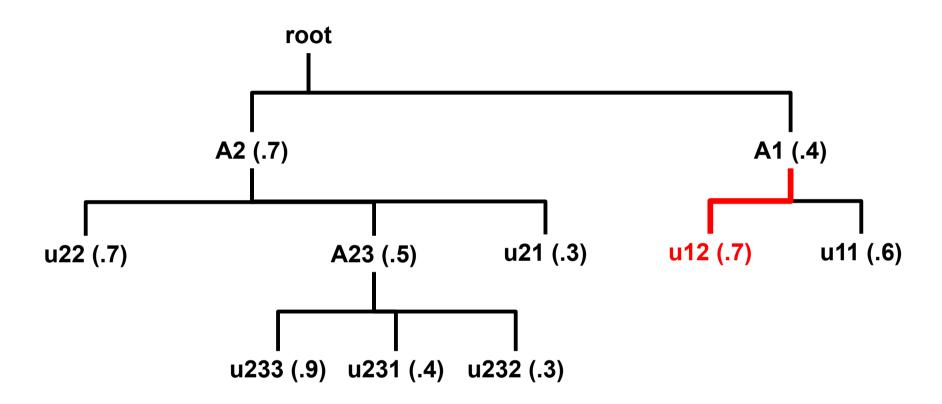


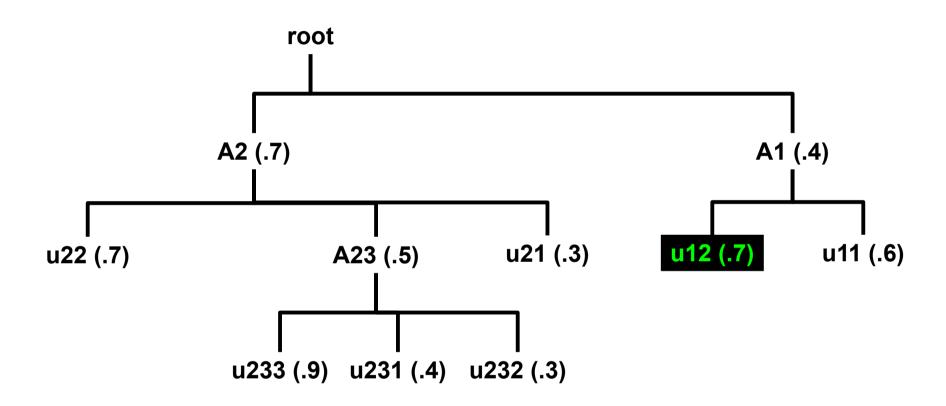




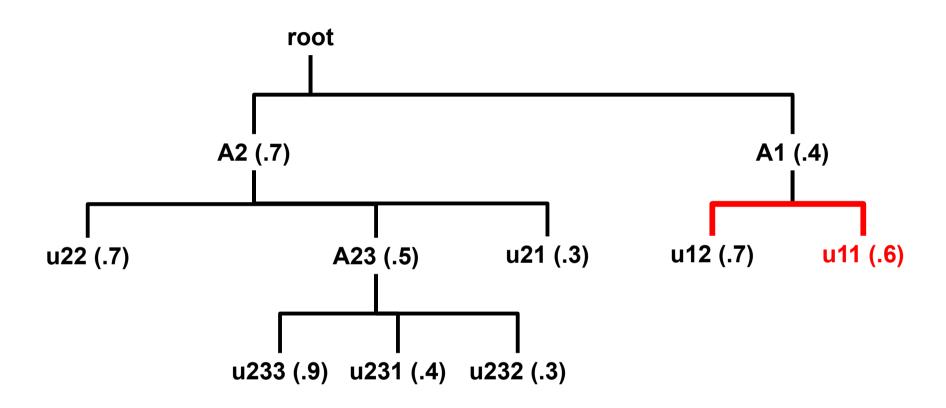




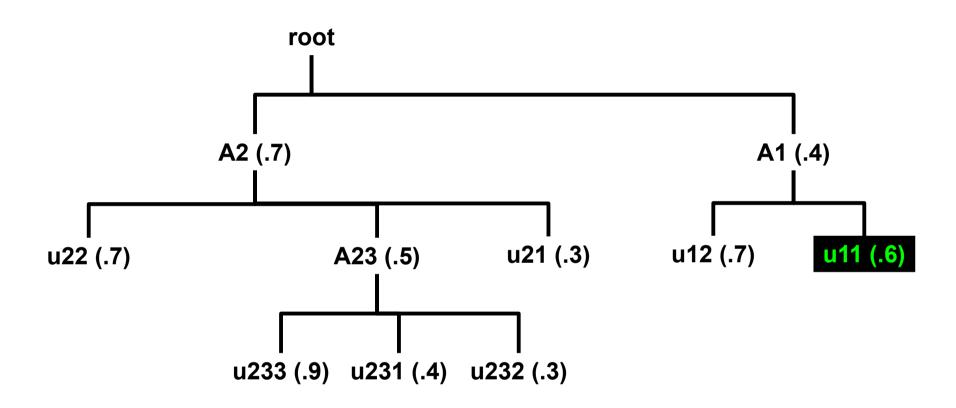




$$0.286 = 2/7$$

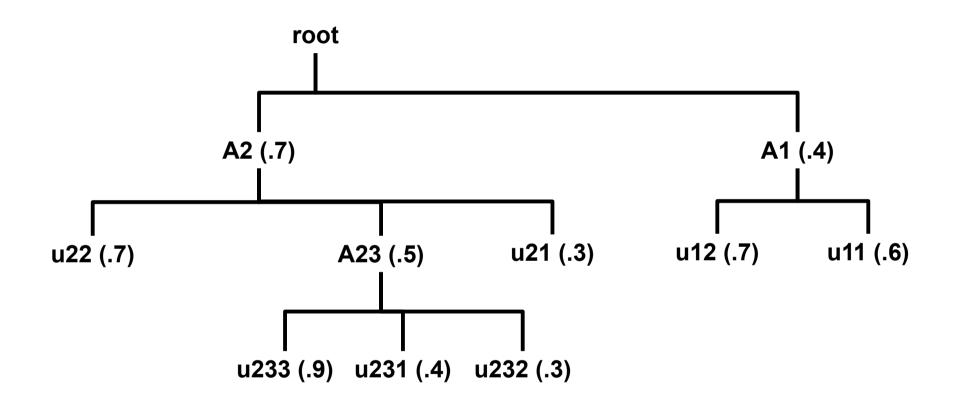


Fair Tree: Traversal



$$0.143 = 1/7$$

Fair Tree: Traversal Complete



Traversal Complete!
All final fairshare values were assigned

Ranking

- Users are ranked as they are found
 - Ties are allowed (e.g. 8,8,8,5,4) if Level Fairshare is equal
 - See the appendix for details of tie handling
- Avoids precision loss

sshare

- Norm Shares and Effectv Usage reflect the Fair Tree approach assoc / (assoc+siblings)
- Level FS (with -I option) Fairshare compared to siblings
- FairShare This is the final fairshare factor (i.e. it works like it should)

Account	User	Raw Shares	Norm Shares	Raw Usage	Norm Usage	Effectv Usage	FairShare	Level FS
root			0.000000	1230		1.000000		1.000000
beatles		500	0.500000	676	0.549593	0.549593		0.909763
beatles	harrison	25	0.250000	301	0.244715	0.445266	0.200000	0.561462
beatles	lennon	25	0.250000	102	0.082927	0.150888	0.600000	1.656863
beatles	mccartney	25	0.250000	37	0.030081	0.054734	0.800000	4.567568
beatles	starr	25	0.250000	236	0.191870	0.349112	0.400000	0.716102
elvis		500	0.500000	554	0.450407	0.450407		1.110108
elvis	elvis	1	1.000000	554	0.450407	1.000000	1.000000	1.000000

^{*}Note: Some sshare columns were cut for brevity in this presentation

Debug

```
      slurmctld:
      Fair Tree fairshare algorithm, starting at root:

      slurmctld:
      elvis (elvis):
      1.11010830324909747294

      slurmctld:
      elvis (elvis):
      1.00000000000000000000000

      slurmctld:
      beatles (beatles):
      0.90976331360946745562

      slurmctld:
      mccartney (beatles):
      4.56756756756756756756756756785

      slurmctld:
      lennon (beatles):
      1.65686274509803921568

      slurmctld:
      starr (beatles):
      0.71610169491525423724

      harrison (beatles):
      0.56146179401993355479
```

- Live view of depth-first traversal
- Users are printed in order of final fairshare factor
- Number shown is Level FS

Easy to Try

- slurm.conf:
 - PriorityFlags=FAIR_TREE
- scontrol reconfigure
 - Wait for next iteration (\$PriorityCalcPeriod minutes)
- Available starting in 14.11.0pre6

Advantages

- Uses entry-level computer science (ordered tree)
- Uses entry-level math
 - S/U is simple
 - LevelFS < LevelFS is simple</pre>
- Precision loss issues extremely unlikely
- Handles unbalanced trees
- Demonstrably fair

Possible Concerns

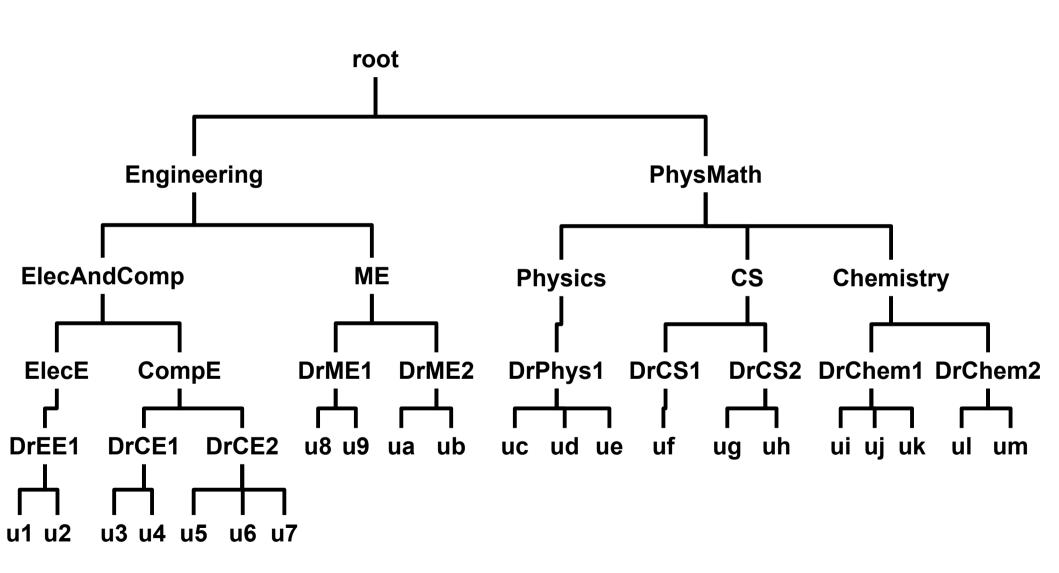
- A user can use all the account's shares if no one else is running
 - (Great!)
 - No algorithm can prevent this
 - User limits (set by admin or account coordinator)
- Tiny user in a very active group has trouble running
 - User will have highest fairshare factor in account but low compared to other accounts
 - Optional QOS w/UsageFactor=20 and Priority=100000000
 - User runs quickly but pays heavily
 - Secondary account with tight limits
- Strictness of hierarchical prioritization
 - Fairshare=parent on accounts
 - Fuzzy matching (see "Future Development")

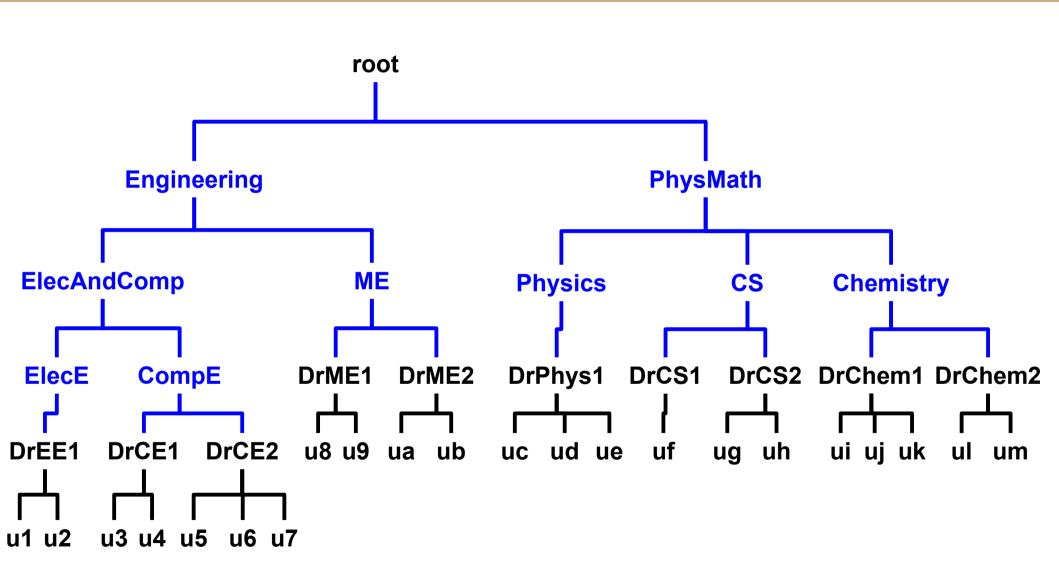
Fairshare=parent modifications (all algorithms)

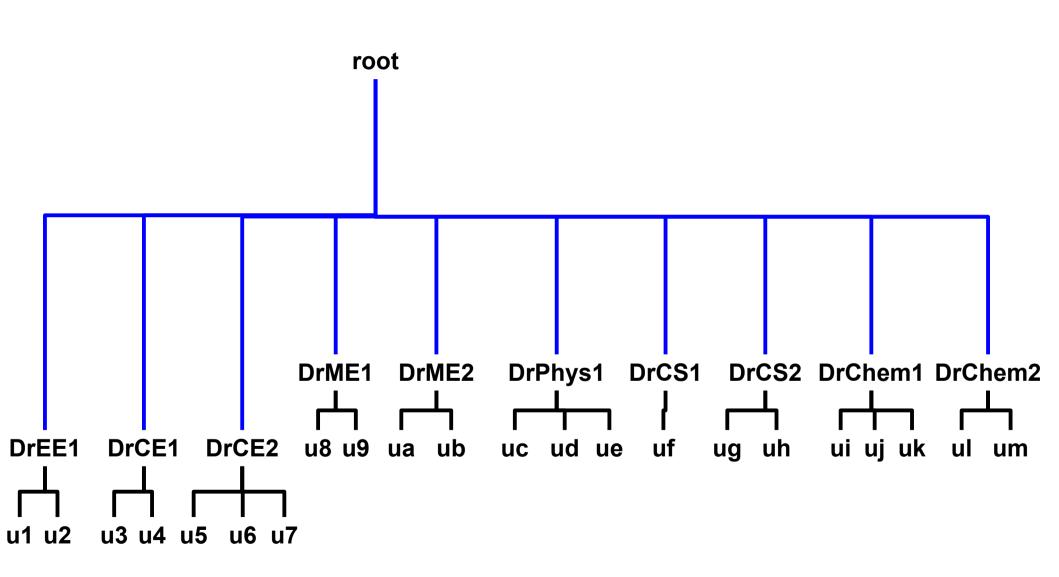
- Fairshare=parent behavior on an <u>account</u> was previously undefined
- It is now defined:

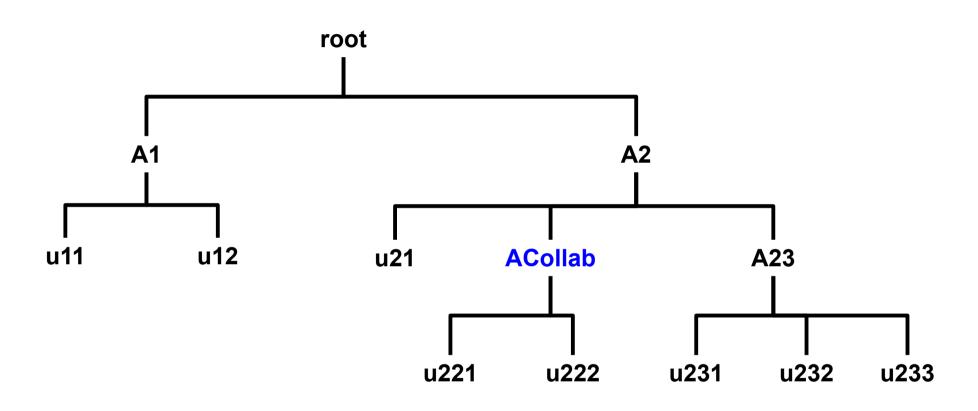
If Fairshare=parent is set on an account, that account's children will be effectively reparented for fairshare calculations to the first ancestor that is not Fairshare=parent.

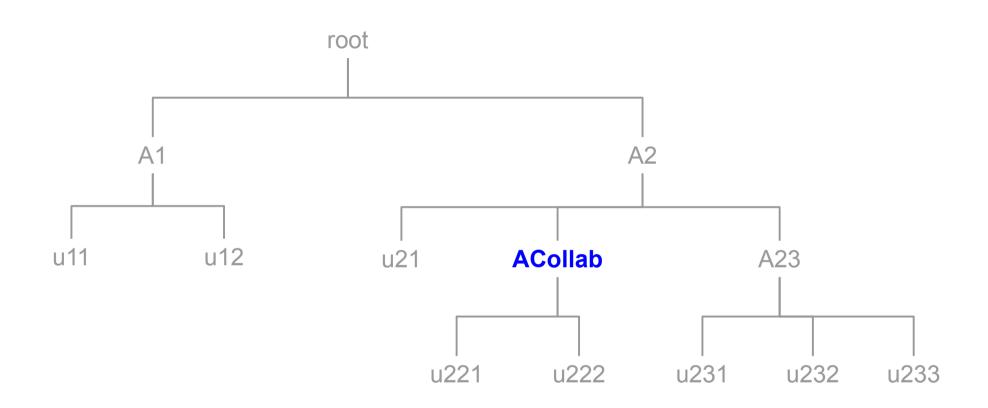
- The behavior of limits is <u>unchanged</u>
- Available in 14.11 for all algorithms





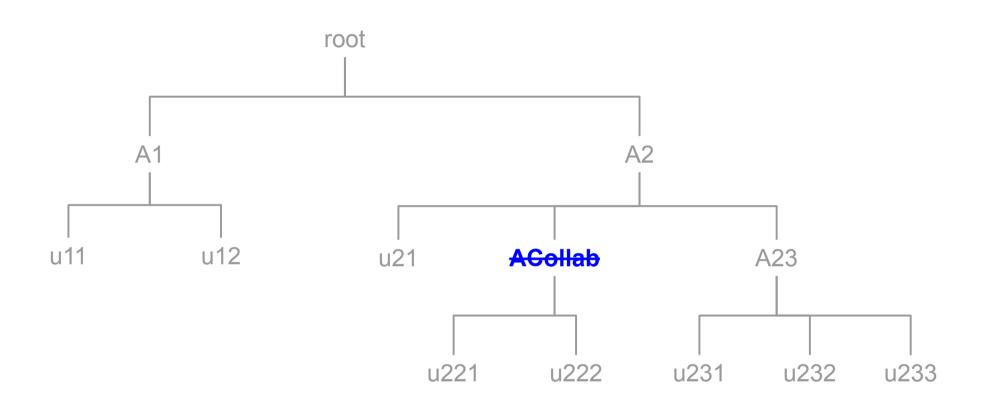






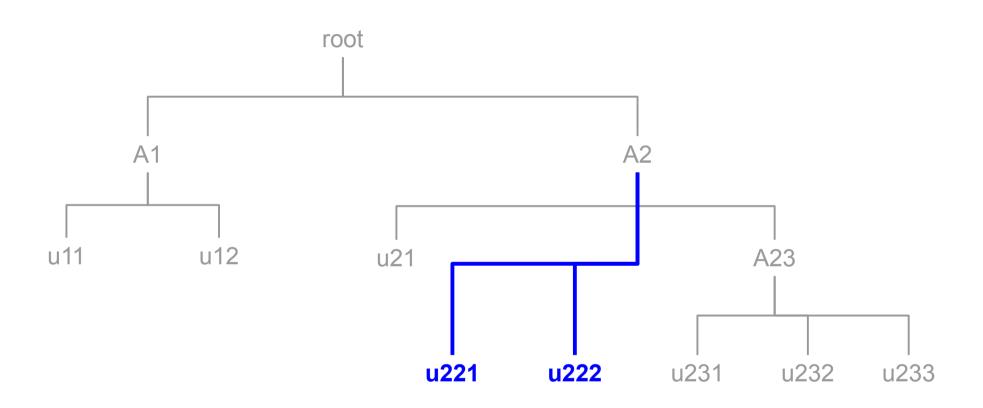
Example:

ACollab is the only association with Fairshare=parent



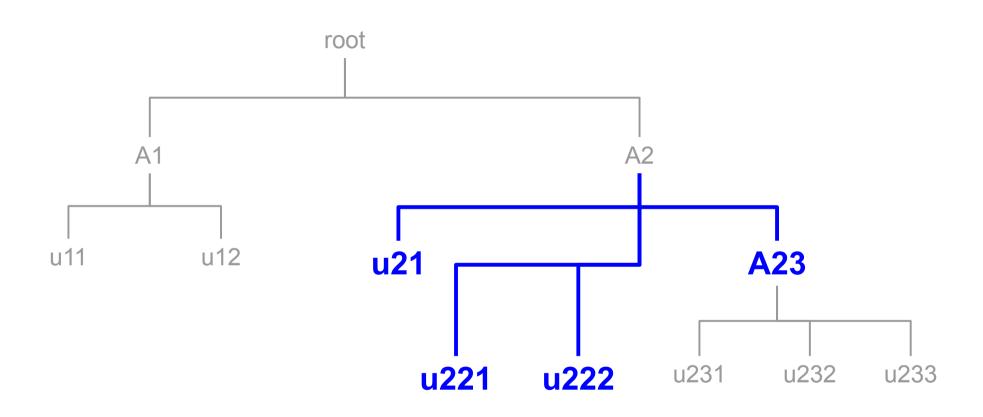
Example:

ACollab effectively disappears

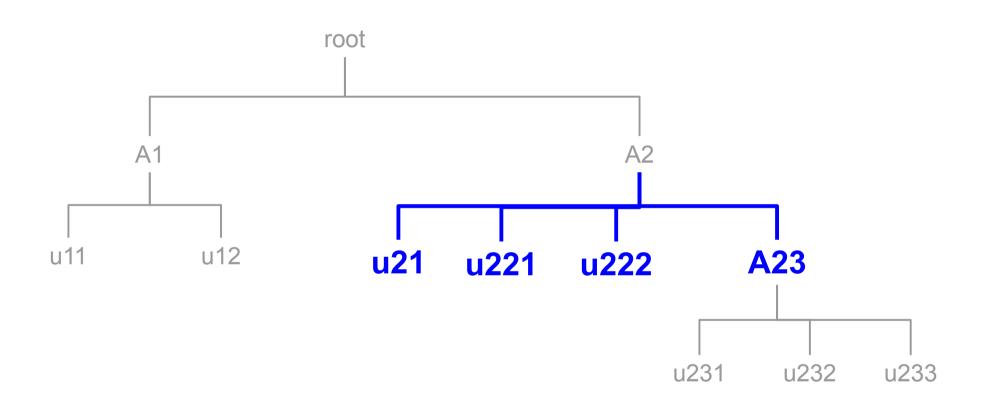


Example:

u221 and u222 are reparented



The following are now **siblings** for purposes of fairshare calculations: u21, u221, u222, A23



The following are now **siblings** for purposes of fairshare calculations: u21, u221, u222, A23

Questions?

Appendix

Appendix Index

- More information
- Future Development
- Problems with Shares Calculation
- Linear Interpolation
- sshare example
- Tie Handling

More Information

- Until 14.11 is released, Fair Tree documentation is at:
 - https://fsl.byu.edu/documentation/slurm/fair_tree.php
- Available in 14.11.0pre6
- Decay is orthogonal to fairshare, i.e. it still works fine
- Contact us if you have questions:
 - ryan_cox@byu.edu
 - levi_morrison@byu.edu
 - slurm-dev list

Future Development

- Allow for less strictness
 - Merge accounts based on configurable delta
 - Allows reuse of tie handling. The comparison function needs a very minor change
 - LevelFSTieDelta=0.01,0.05,0.02
 - Values are the epsilon value at increasing depths
 - Either:
 - a > b * (1 delta) && a < b * (1 + delta)
 - abs((a b) < delta)

$$S = (S_{user} / S_{siblings}) *$$

$$(S_{account} / S_{sibling-accounts}) *$$

$$(S_{parent} / S_{parent-siblings}) * ...$$

Normalized Shares equation for all current algorithms:

$$S = (S_{user} / S_{siblings}) *$$

$$(S_{account} / S_{sibling-accounts}) *$$

$$(S_{parent} / S_{parent-siblings}) * ...$$

Example:

- The tree is no deeper than: root->account->user
- Assume sibling associations are treated equally (same Shares)
- Problem still applies for more complicated scenarios

$$S = (S_{user} / S_{siblings}) *$$

$$(S_{account} / S_{sibling-accounts}) *$$

$$(S_{parent} / S_{parent-siblings}) * \dots$$

- The tree is no deeper than: root->account->user
- Therefore:

$$S = (S_{user} / S_{siblings}) * (S_{account} / S_{sibling-accounts})$$

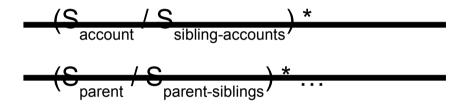
$$S = (S_{user} / S_{siblings}) *$$

$$(S_{account} / S_{sibling-accounts}) *$$

$$(S_{parent} / S_{parent-siblings}) *$$

- If each account is Shares=500
- $S_{account} / S_{sibling-accounts} = 500 / (500 * count(accounts))$
- S_{account} / S_{sibling-accounts} = 1 / count(accounts)
- This is a constant for <u>all</u> accounts

$$S = (S_{user} / S_{siblings}) * constant$$

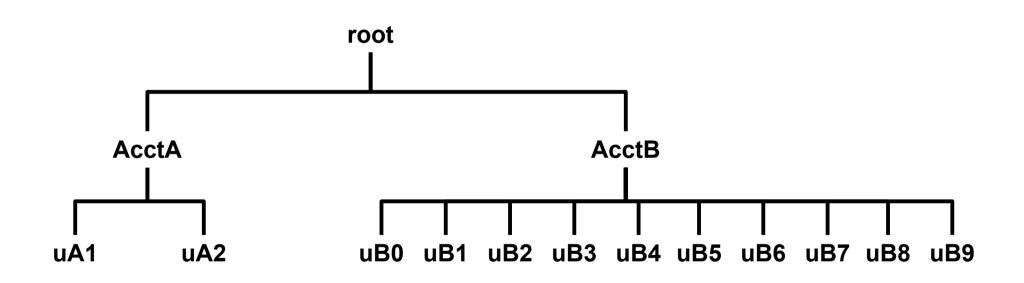


- $S = (S_{user} / S_{siblings}) * constant$
- Since we are comparing... constants are thrown out:
- $S = (S_{user} / S_{siblings})$

- If each user is Shares=100
- S = 100 / (100 * count(users_in_account))
- S = 1 / count(users_in_account)

 Normalized Shares equation for all current algorithms when accounts are treated equally and users in an account are treated equally:

The problem still exists for other scenarios but is harder to model



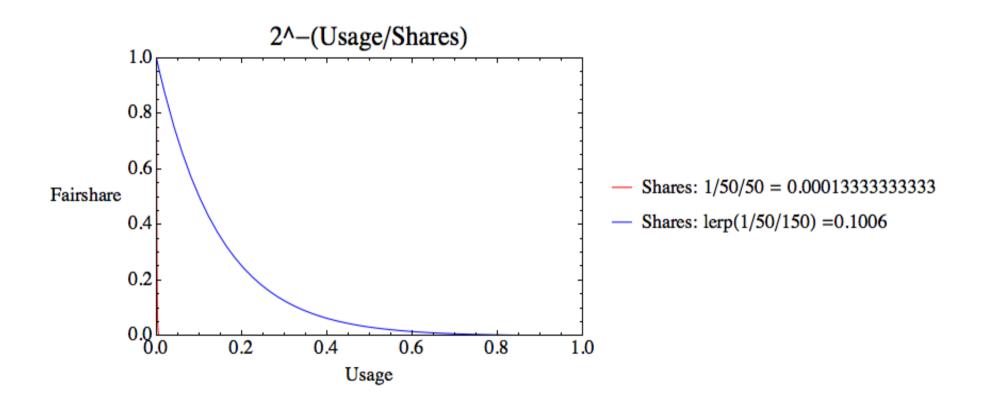
$$S = 1/2 = 0.5$$

$$S = 1/10 = 0.1$$

Linear Interpolation (lerp)

- Shares are between 0.0 .. 1.0
- Map them to the range 0.1 .. 1.0
 - Use linear interpolation (lerp)
- lerp(min, max, f) = min + f * (max min)
 - Has floating point issues
- lerp(min, max, f) = min * (1.0L f) + max * f
 - Shouldn't have floating point issues
- lerp(0.1, 1.0, 0.00001) = 0.100009

Linear Interpolation (lerp)



Unmodified vs lerp()

Usage	Shares	Fairshare (unmodified)	Fairshare (lerp)
0.15	.2	0.59460355750136062447097629046766	0.68981706017270247755391460176000
0.15	.1	0.35355339059327384187980669594253	0 .57855511864135993283170603107557
0.15	.02	0.00552427172801990291201024163570	0 .41431890600793676033685580817334
0.15	.01	0.000030517578125000000000000000000	0 .38524635476490996013063453085046
0.15	.002	0.0000000000000000000000000000000000000	0.3 6011325130027945195512403819826
0.15	.001	0.0000000000000000000000000000000000000	0.35684750329912502426078085848715
0.15	.0002	0.0000000000000000000000000000000000000	0.35421449328863424725827649397480
0.15	.0001	0.0000000000000000000000000000000000000	0.35388408479113951296806533930450
0.15	.00000000002	0.0000000000000000000000000000000000000	0.35355339065944120049999645216676
0.15	.0000000001	0.0000000000000000000000000000000000000	0.35355339062635748816239289471497

- Fairshare factor is multiplied by PriorityWeightFairshare, making the problem much worse
- If lerp() is implemented, add an option (-L?) to sshare:
 - change Norm Shares → Lerp Shares

sshare

- Norm Shares and Effectv Usage reflect the Fair Tree approach assoc / (assoc+siblings)
- Level FS (with -l option) Fairshare compared to siblings
- FairShare This is the final fairshare factor (i.e. it works like it should)

Account	User	Raw Shares	Norm Shares	Raw Usage	Norm Usage	Effectv Usage	FairShare	Level FS
root			0.000000		0 = 40=00	1.000000		1.000000
beatles		500	0.500000	676	0.549593	0.549593		0.909763
beatles	harrison	25	0.250000	301	0.244715	0.445266	0.200000	0.561462
beatles	lennon	25	0.250000	102	0.082927	0.150888	0.600000	1.656863
beatles	mccartney	25	0.250000	37	0.030081	0.054734	0.800000	4.567568
beatles	starr	25	0.250000	236	0.191870	0.349112	0.400000	0.716102
elvis		500	0.500000	554	0.450407	0.450407		1.110108
elvis	elvis	1	1.000000	554	0.450407	1.000000	1.000000	1.000000

McCartney: Why do I have a lower fairshare factor than Elvis?

^{*}Note: Some sshare columns were cut for brevity in this presentation

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Answer: Compare the accounts' Level FS values

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McCartney: How is Level FS calculated?

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Answer: Norm Shares / Effectv Usage

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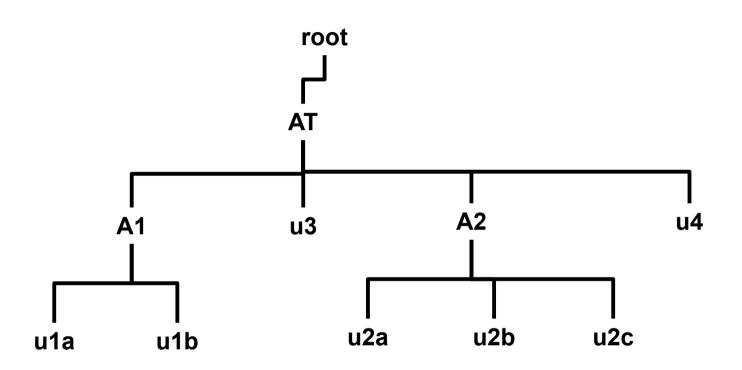
Account	User	Raw Shares	Norm Shares	Raw Usage	Norm Usage	Effectv Usage	FairShare	Level FS
root beatles		500	0.000000	1230 676	0.549593	1.000000		1.000000
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Answer: Norm Shares / Effectv Usage

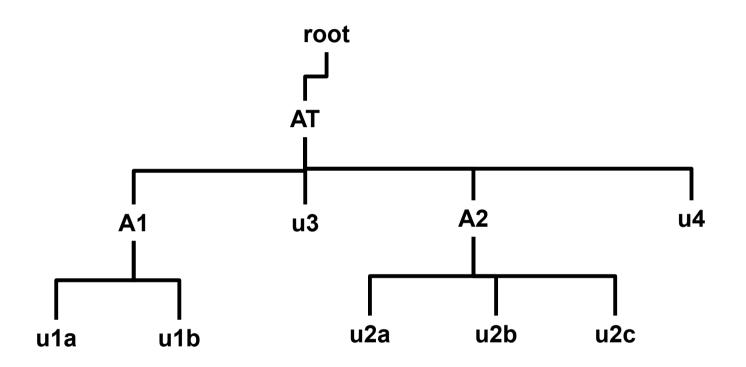
^{*}Note: Some sshare columns were cut for brevity in this presentation

Ties

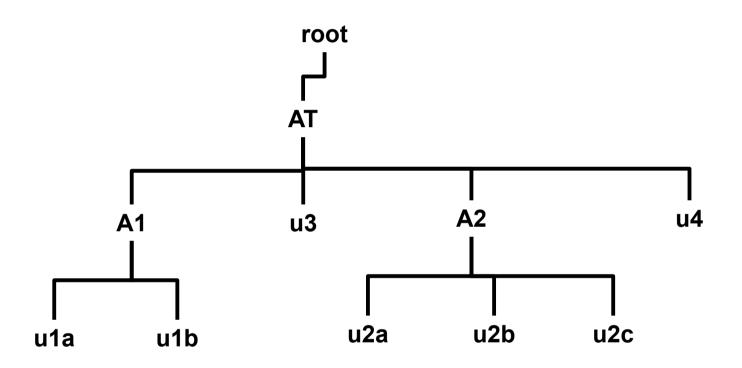
- Occur when sibling associations have the same level_fs
 - Extremely rare except when raw usage == 0.0
 - Added complexity to the code
- Rules:
 - Sibling users receive the same rank
 - Sibling accounts have their children lists merged
 - A user with the same level_fs as a sibling account will receive the same rank as the account's highest ranked user



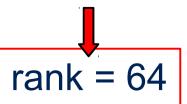
This is one portion of the tree. AT is pictured in its entirety.

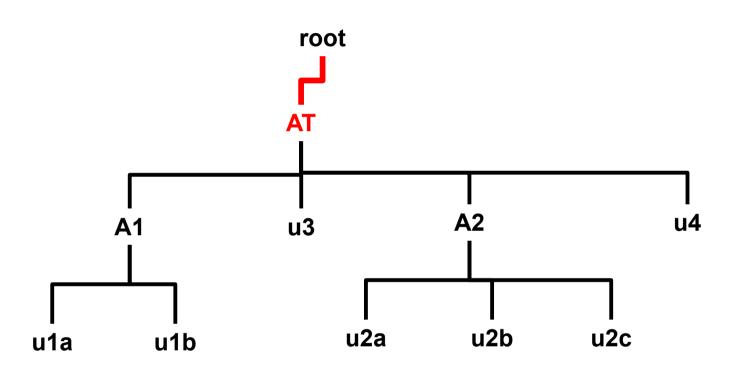


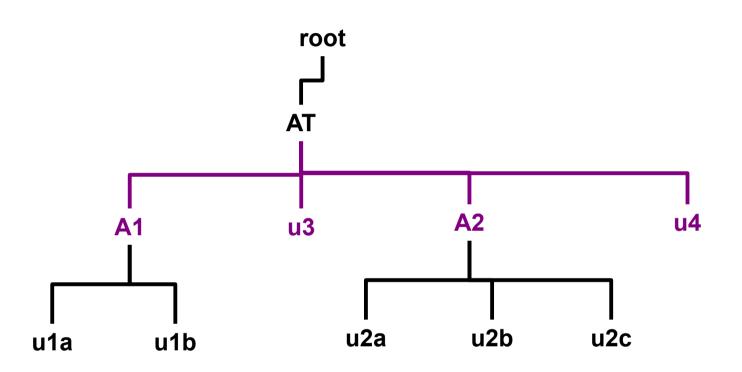
There are 83 users (not all pictured). Some have been visited.

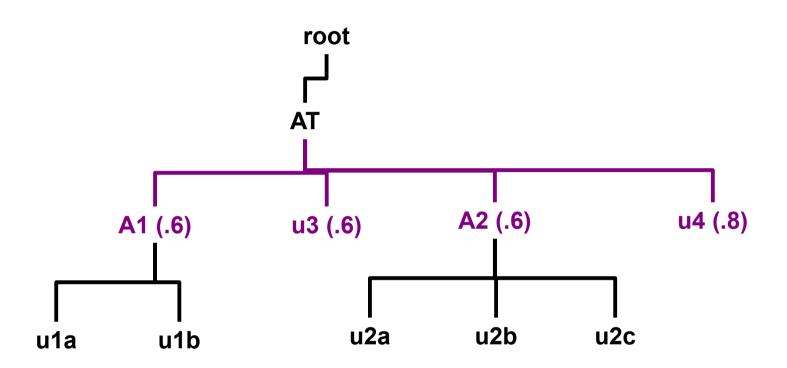


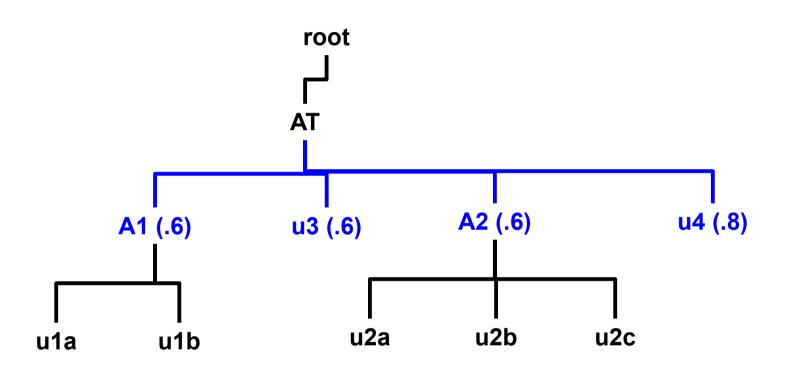
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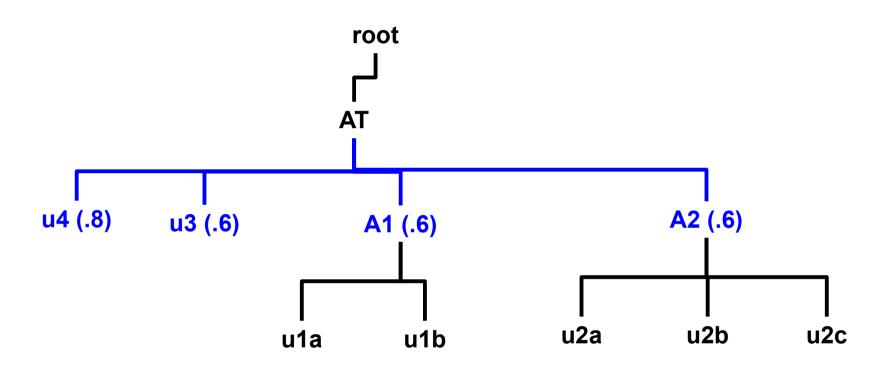


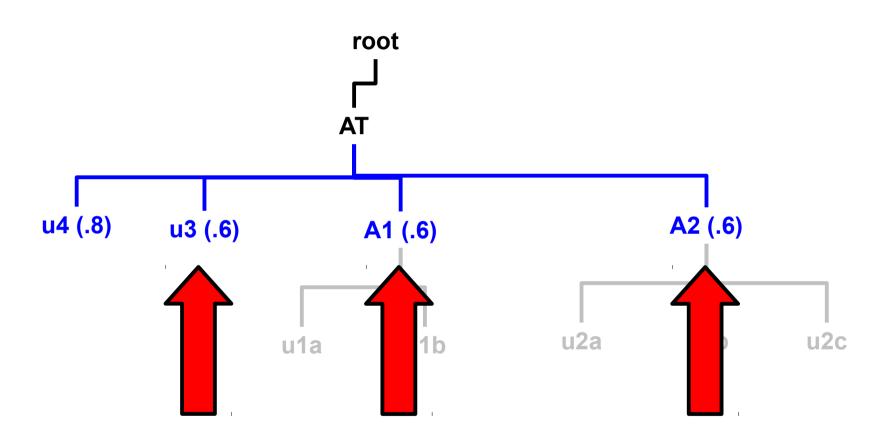




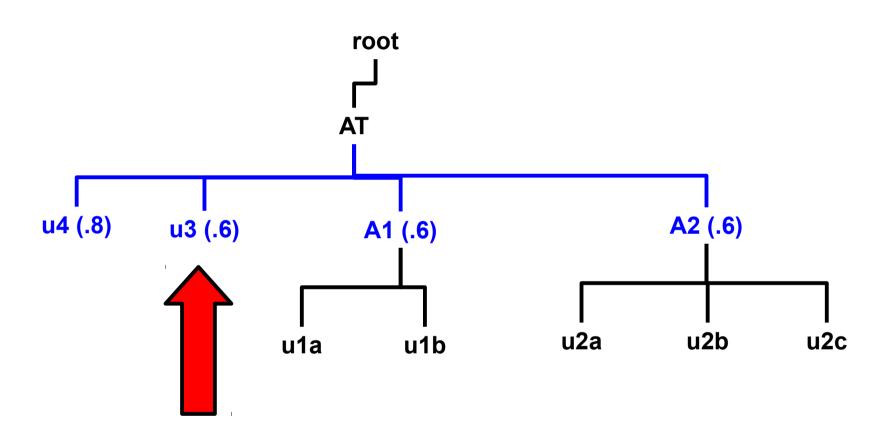






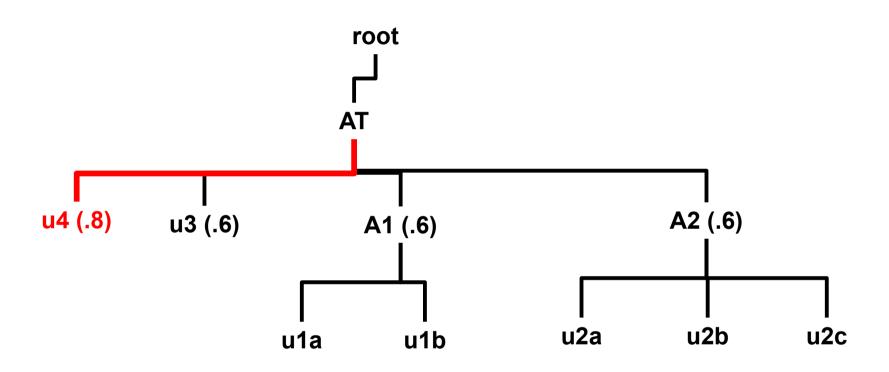


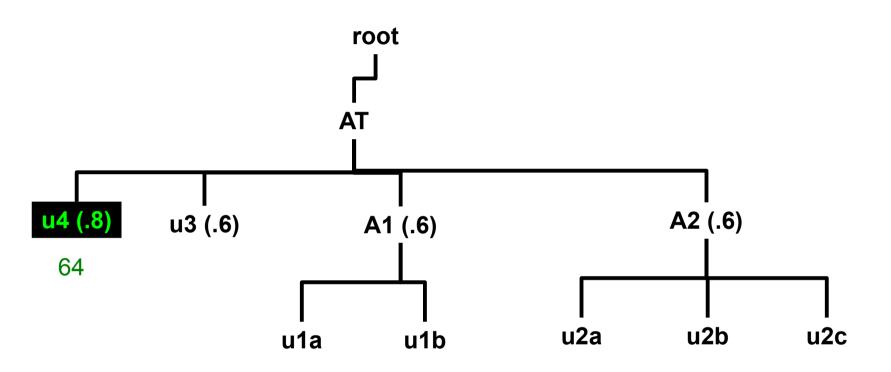
u3, A1, and A2 are tied at .6

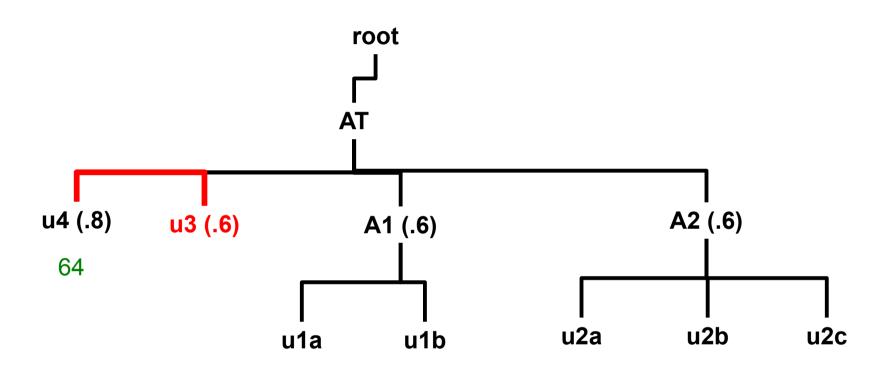


Tied users are placed to the left

$$rank = 64$$

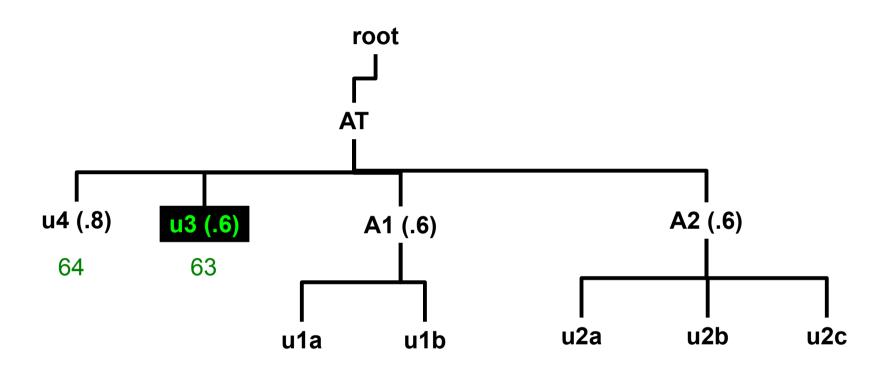


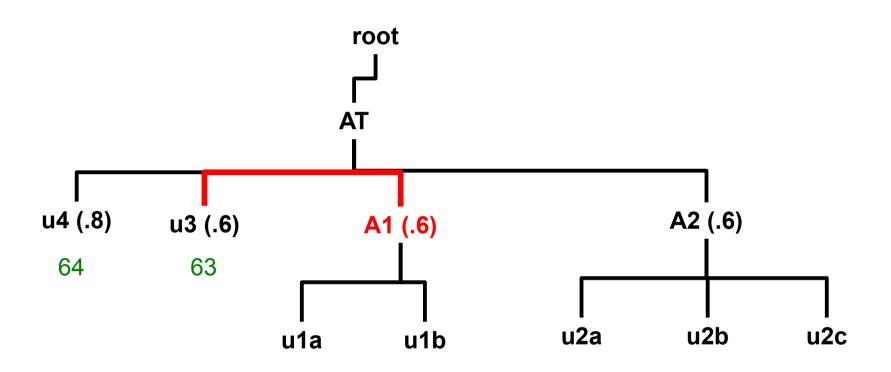




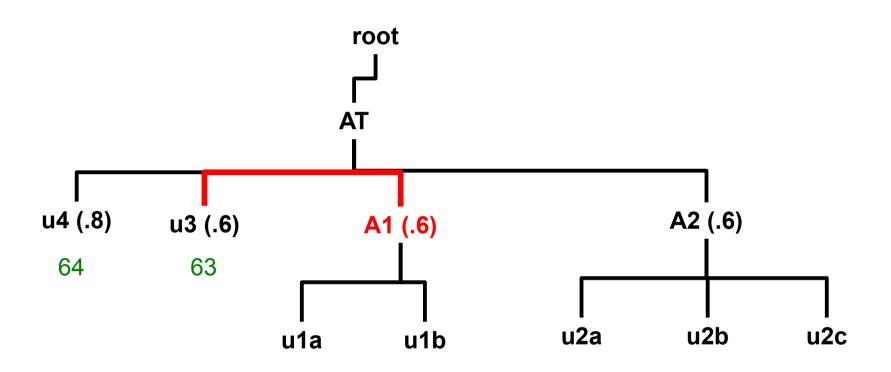
Next association **not** tied. Decrement rank.



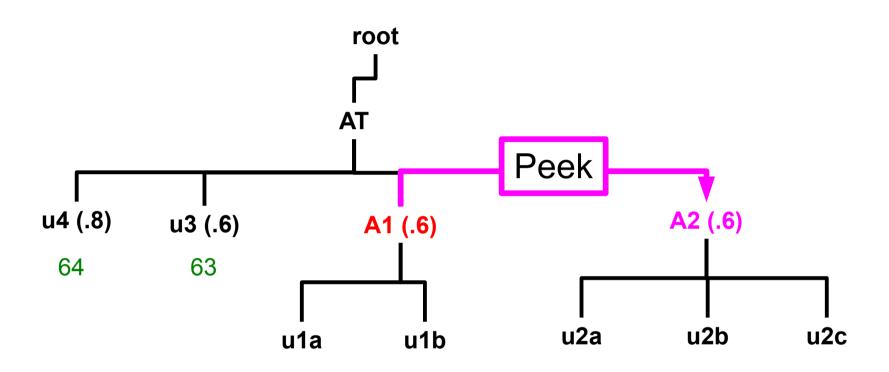




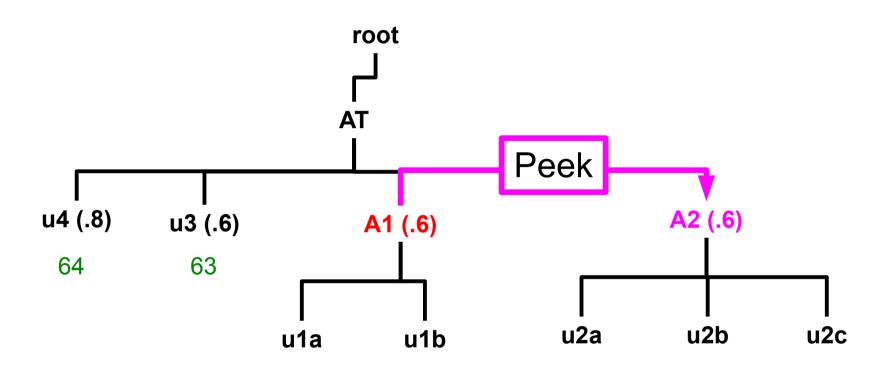
Next association is tied. rank stays the same



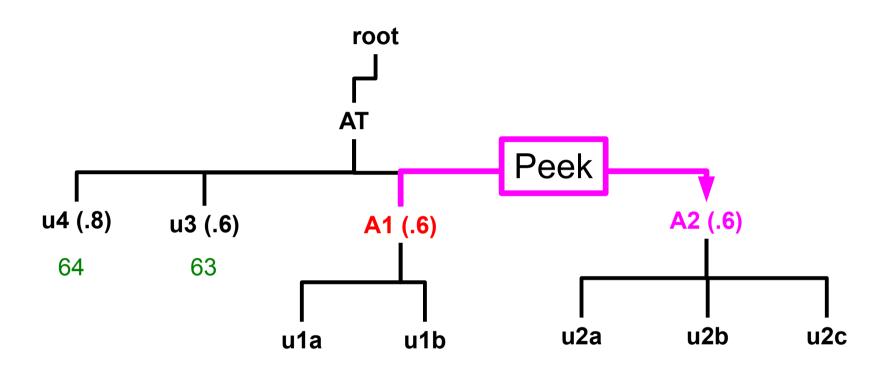
Next association is tied. rank stays the same



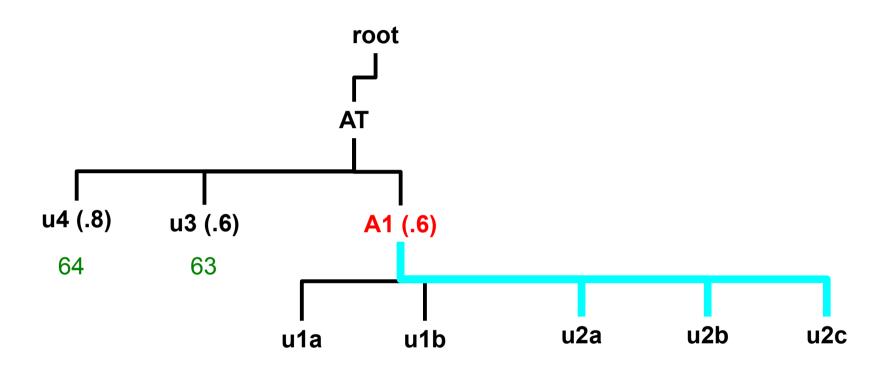
Peek at next account to check for a tie



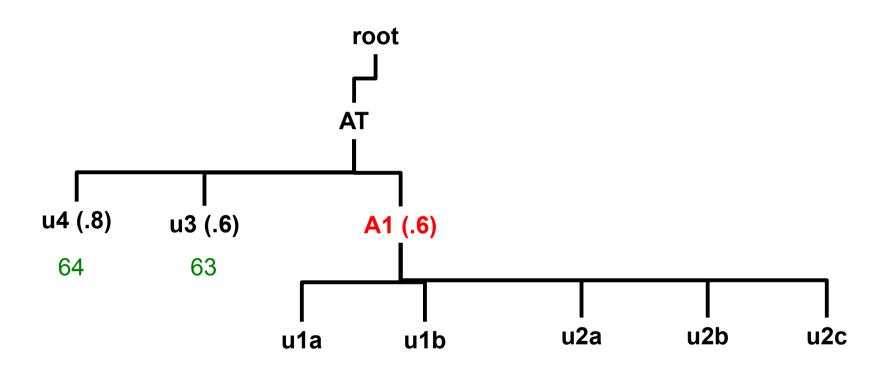
A1->level_fs == A2->level_fs



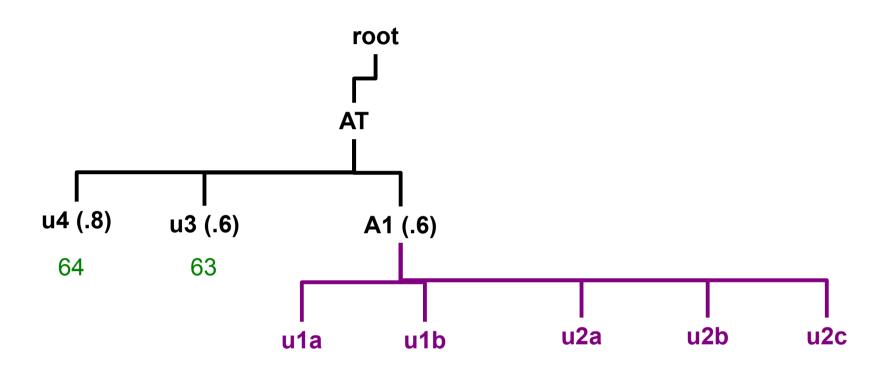
Accounts are equal. Merge!



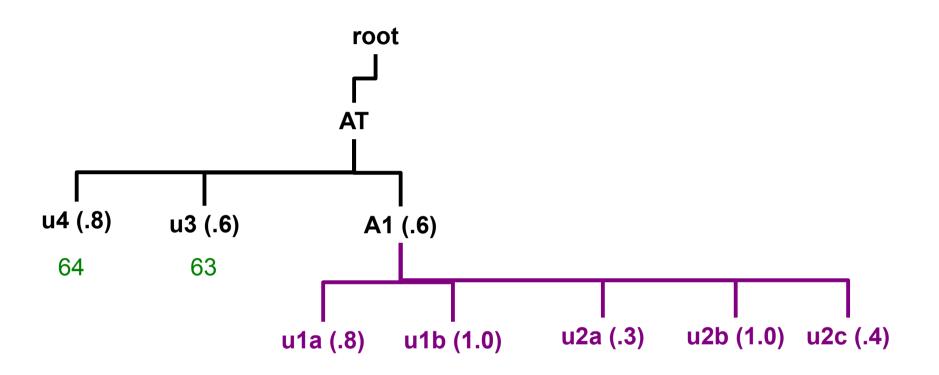
Merge complete



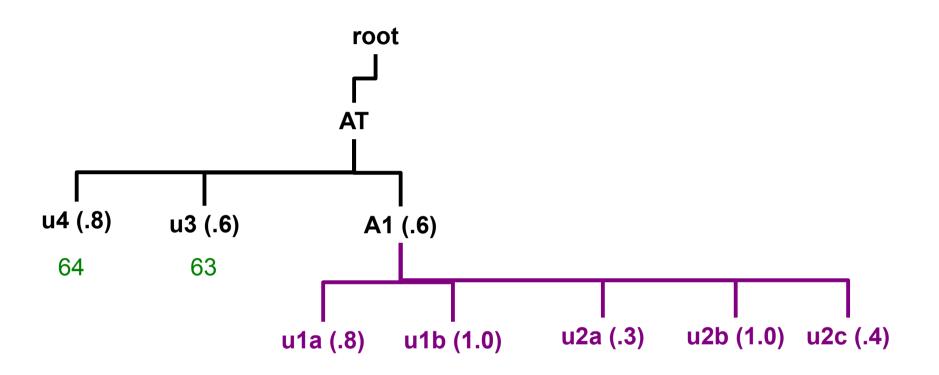
Merge complete



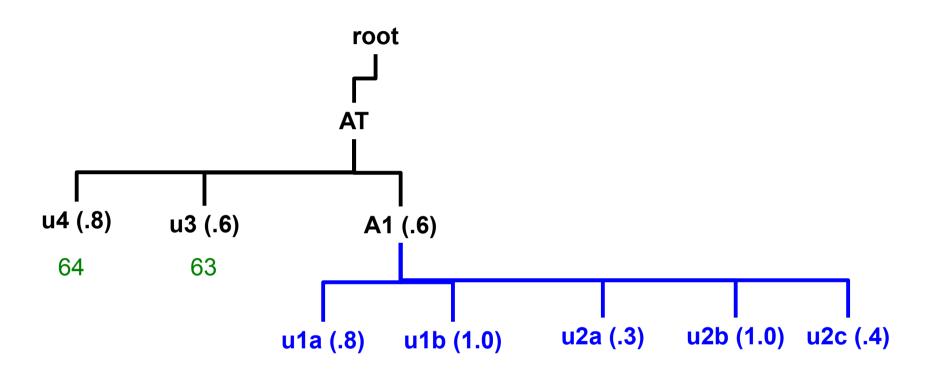
Calculate level_fs using **actual siblings**, <u>not</u> adopted ones. The calculations pretend that the merge never happened.



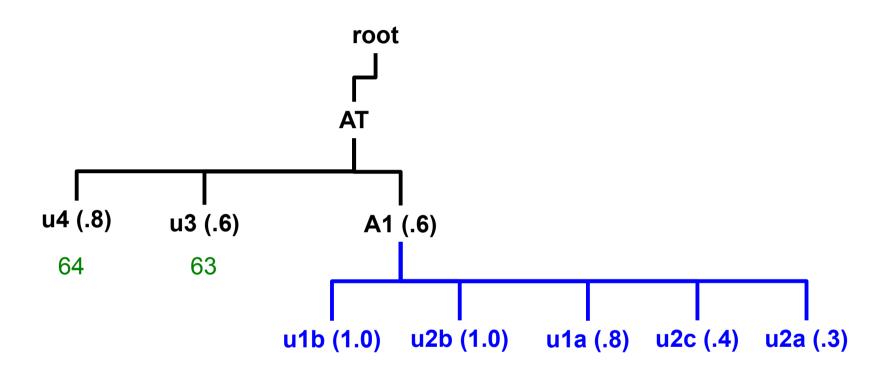
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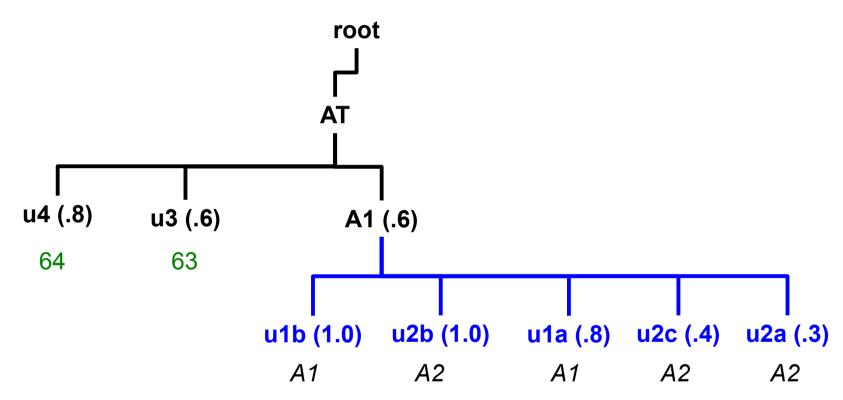
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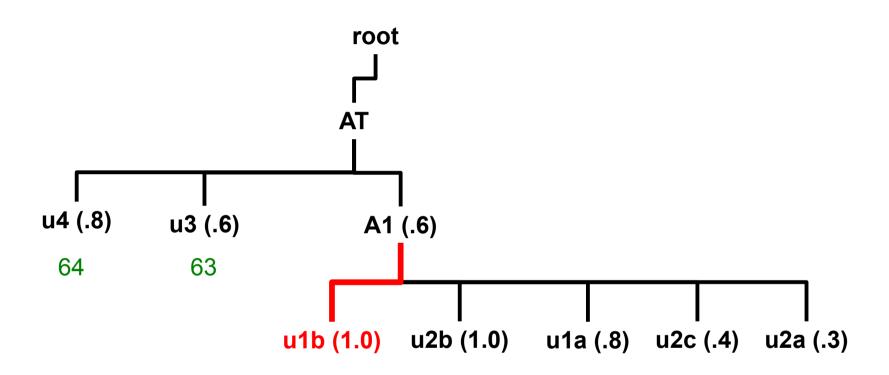
Sorting uses the merged list

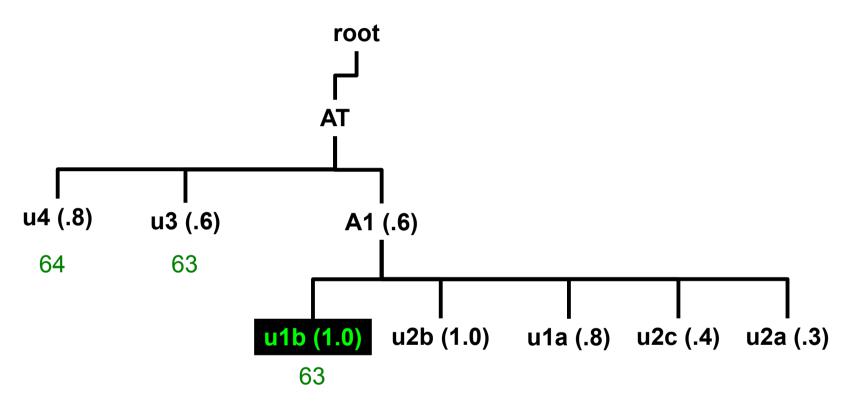


Sorting uses the merged list

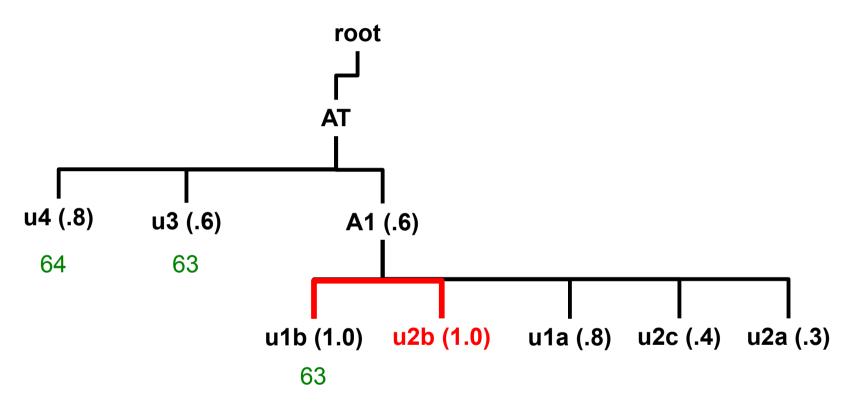


Note that the merged users are mixed

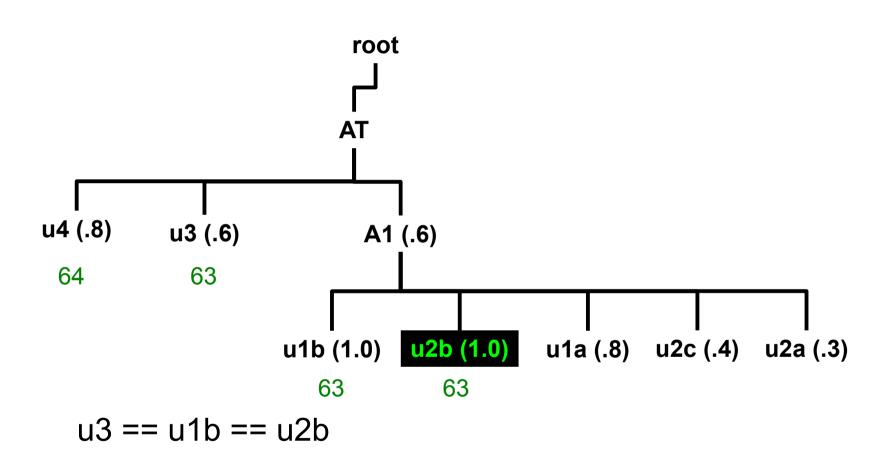


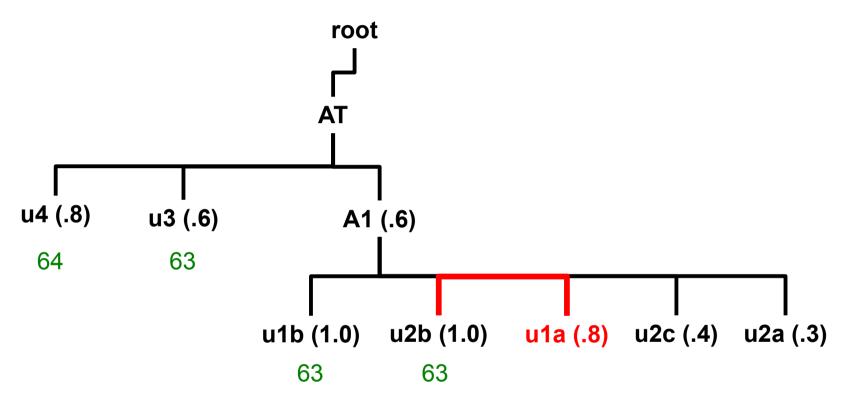


Note that rank has **not** been decremented. u1b receives the same rank as u3 since A1 tied u3.



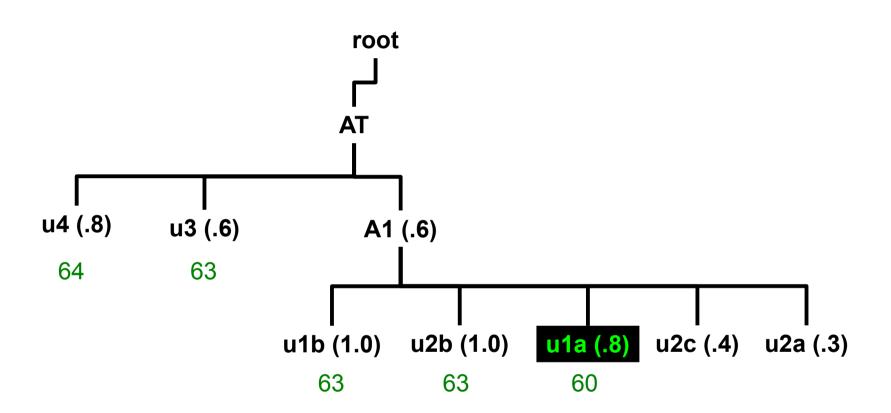
Next association is tied. Rank stays the same

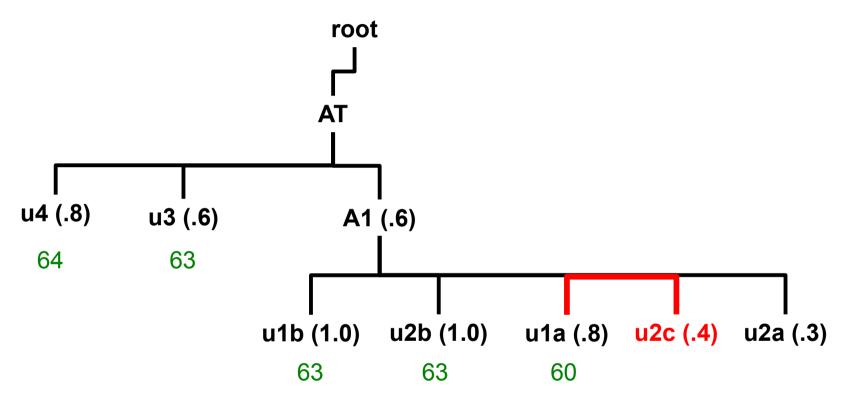




Next association **not** tied. Decrement rank by 3 (3 ties)

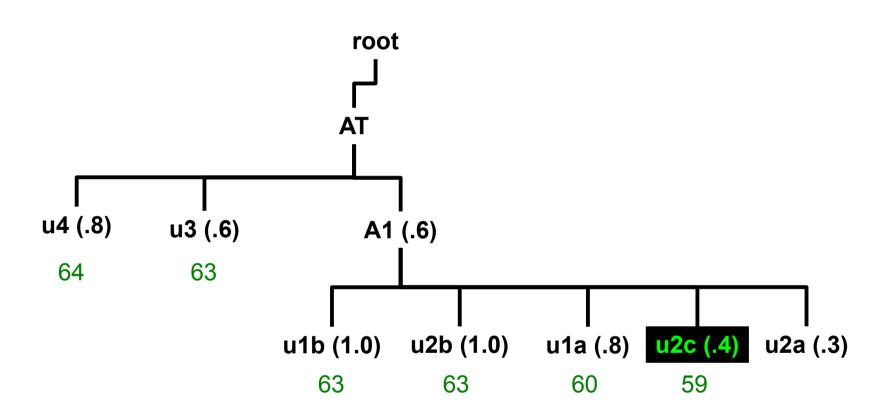


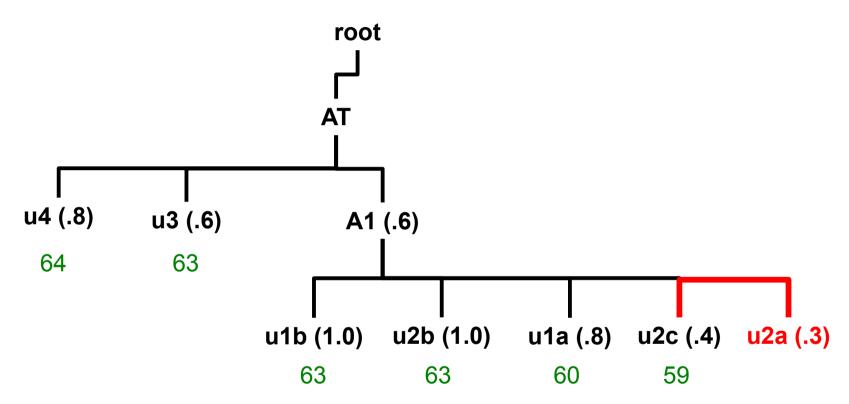




Next association **not** tied. Decrement rank

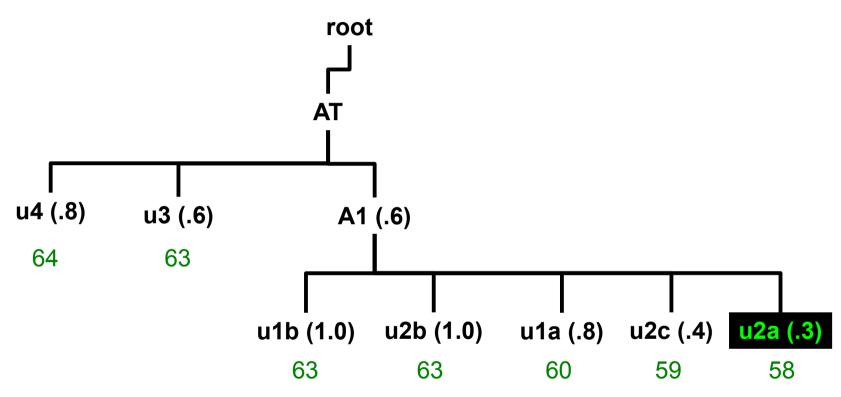




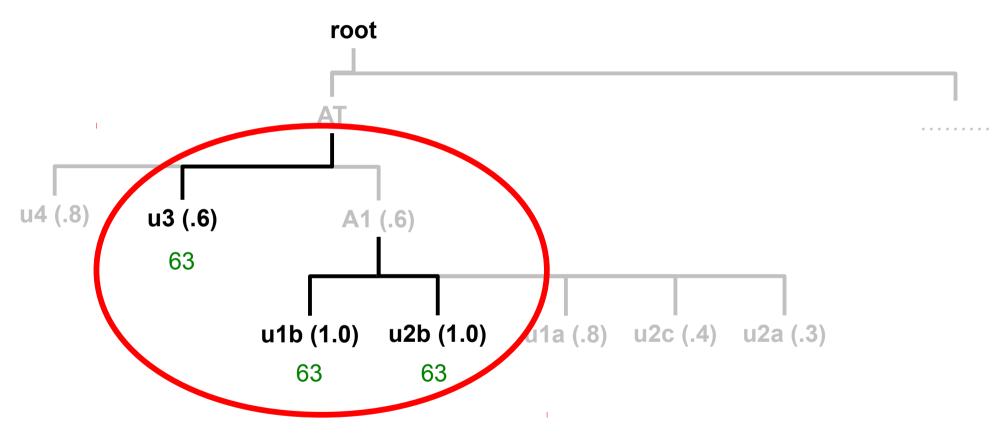


Next association **not** tied. Decrement rank

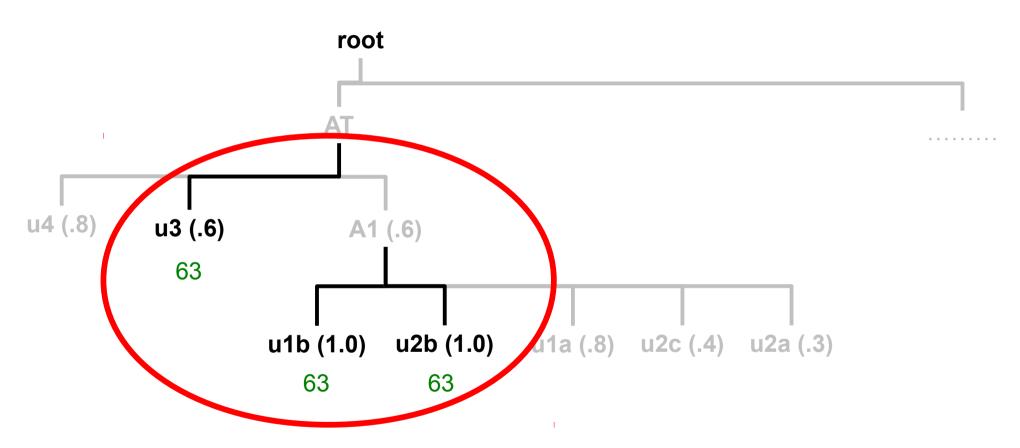




Sorting uses the merged list



u3, u1b, and u2b receive equal rankings



- u3 tied A1, thus it tied A1's highest rank user, u1b
- u1b tied its adopted sibling user, u2b, since A1 and A2 were tied
- u3, u1b, and u2b receive the same fairshare factor